

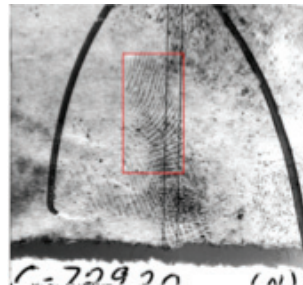
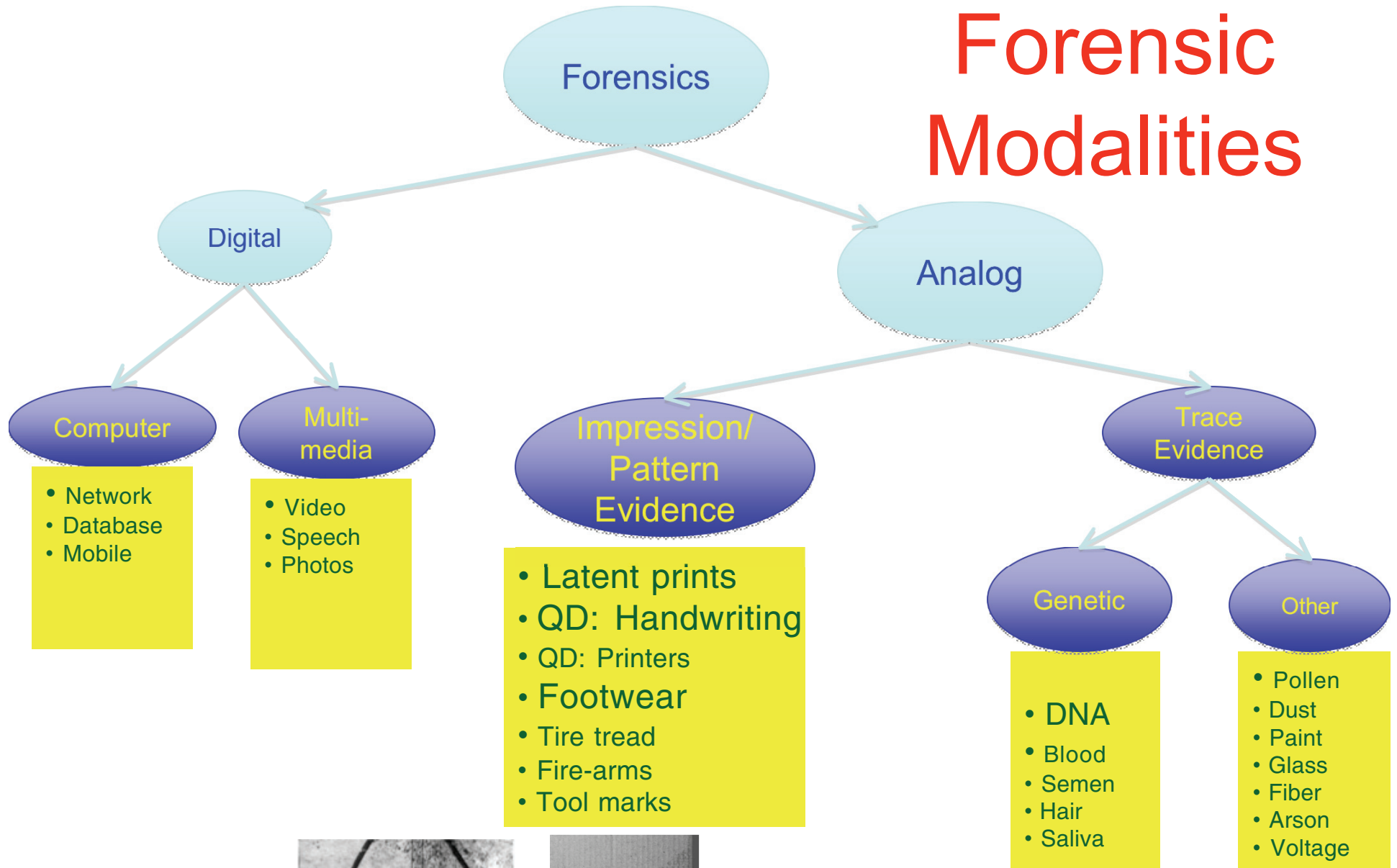
# Probability Models for Impression and Pattern Evidence

Sargur Srihari

Department of Computer Science and Engineering  
University at Buffalo, The State University of New York

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# Forensic Modalities



# Forensic Opinion

- Courts allow Latent Print Examiner to opine on ultimate question of individualization
  - Evidence is attributed to a single individual and no other
- Three possible opinions
  - The evidence
    - Individualizes
      - No other individual on earth
    - Inconclusive
    - Excludes
      - Definitely not this individual

# Madrid Bombing Case

Latent Fingerprint  
on bag of detonator



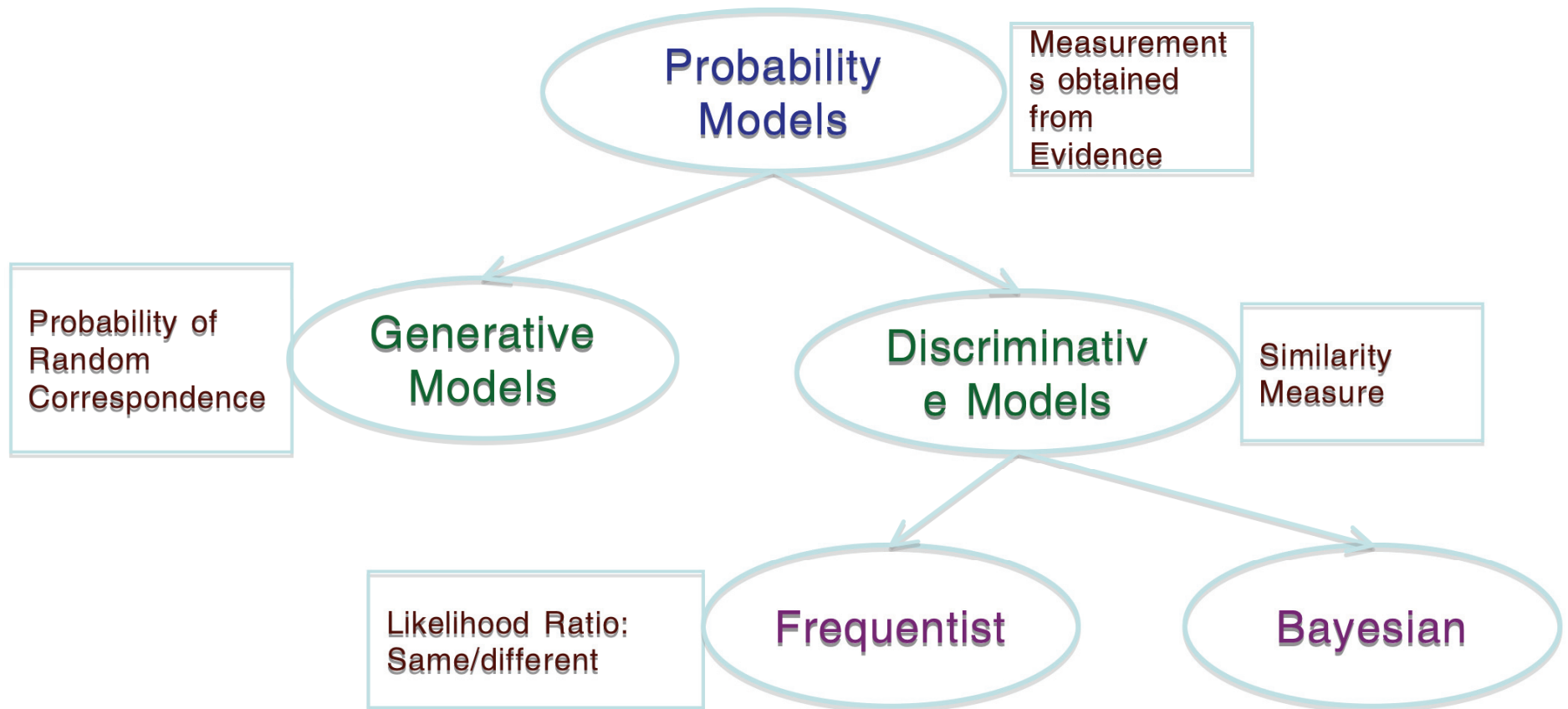
Brandon Mayfield  
Identified by FBI



Algerian National  
Identified by SNP



# Methods for Expressing Uncertainty



# How to Compute Uncertainty?

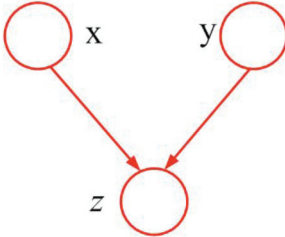
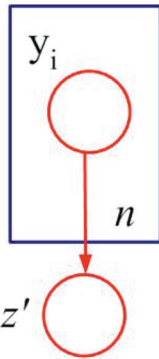
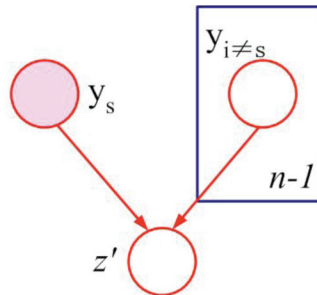
- Discrete Variables
  - Birthdays
  - DNA
- Continuous Variables
  - Heights
  - Pattern/Impression evidence (Ongoing Research)
    - 5 or 9-point scale suggested by SWGs-- no guidelines
    - New statistical models being developed

# Generative Models: Several Probabilities

Random two have same birthday ( $n=2$ )

Some two among  $n$  have same birthday

A specific birthday among  $n$

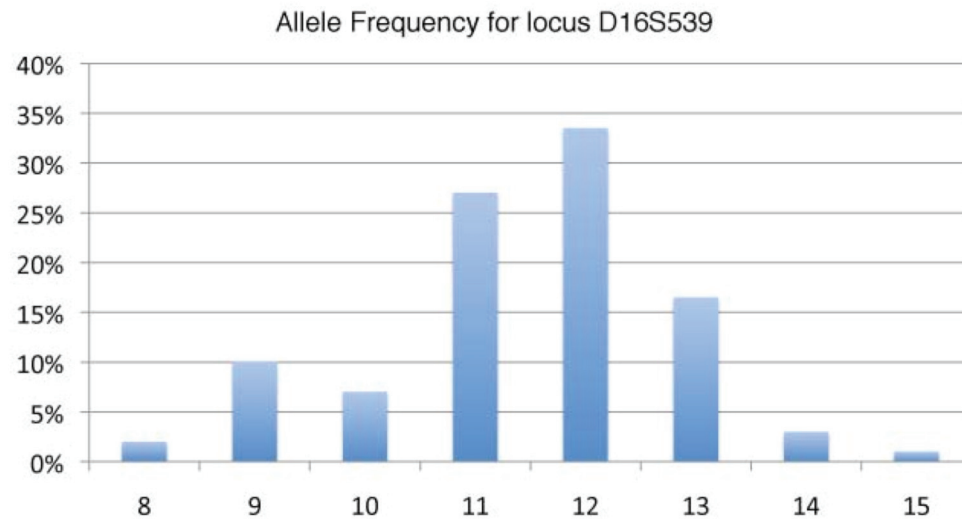
	PRC	nPRC	Specific nPRC
Graphical Model	 <p>(a)</p> $z = \{1, 0\}$	 <p>(b)</p> $z' = \{1, 0\}$	 <p>(c)</p> $z' = \{1, 0\}$
Inference	$p(z) = \sum_{\mathbf{x}} \sum_{\mathbf{y}} p(z \mathbf{x}, \mathbf{y}) p(\mathbf{x}) p(\mathbf{y})$ <p>PRC is <math>\rho^{\bar{=}} p(z=1)</math></p>	$\rho[n] = 1 - (1 - \rho)^{\frac{n(n-1)}{2}}$	$p(z' y_s) = \sum_{Y'} p(z', Y' y_s) = \sum_{Y'} p(z' y_s, Y') p(Y')$





# Generative Model: DNA

Allele Frequency of single locus for 200 individuals



DNA profile of 13 loci:

Average match probability (PRC) is 0.1 per locus,  $10^{-13}$  for a profile

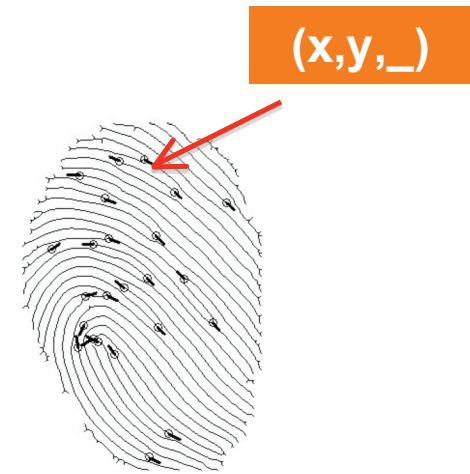
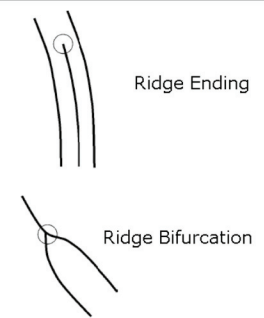
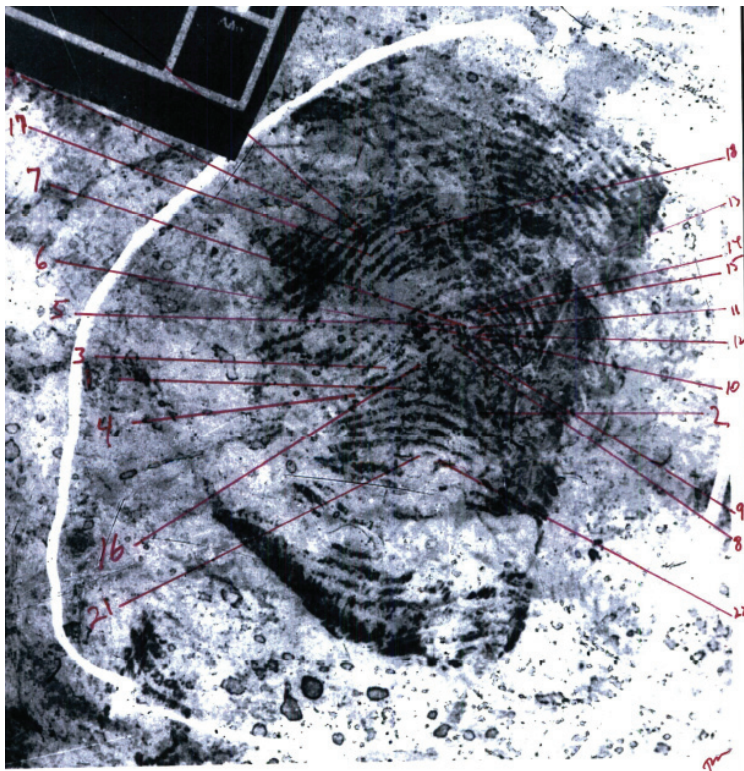
If database has 1 million entries,

since there are 500 billion pair-wise matches,  $nPRC = 0.05$

However specific  $nPRC$  can be much lower

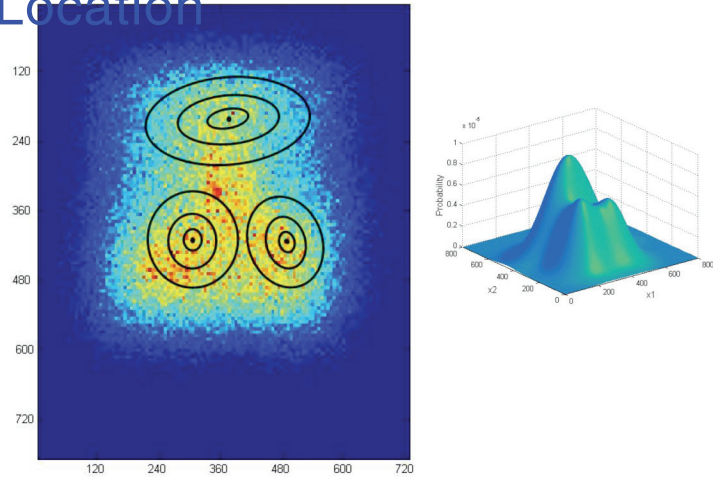
# Generative Models: Fingerprints

- Fingerprints are characterized by ridges and minutiae

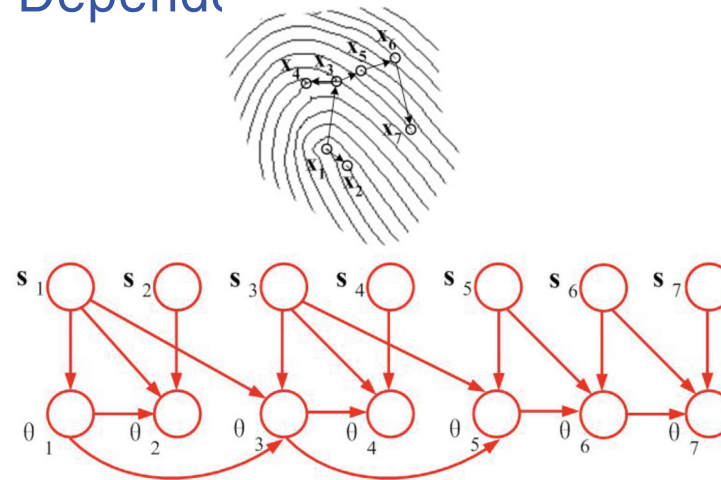


# Generative Model: Minutiae

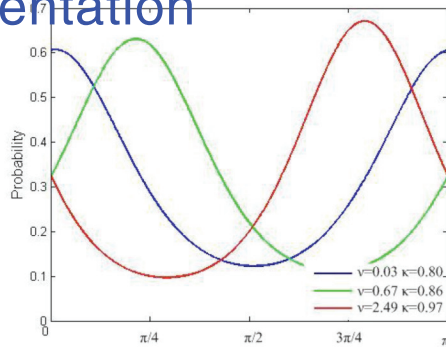
## 1. Distribution of Minutia Location



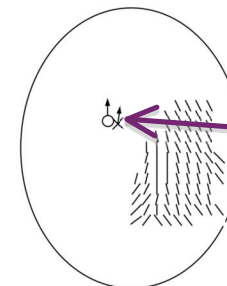
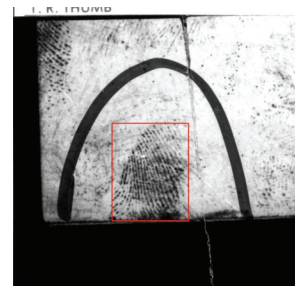
## 3. Distribution of Minutia Dependency



## 2. Distribution of Minutia Orientation

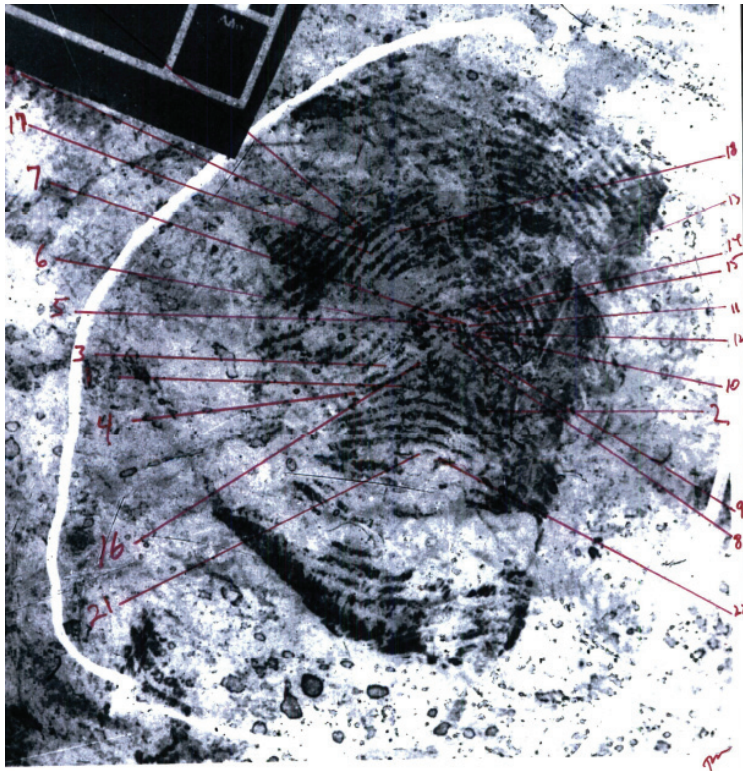


## 4. Distribution of Minutia Certainty



Core point predicted Using Regression

# Madrid Bomber Case Revisited

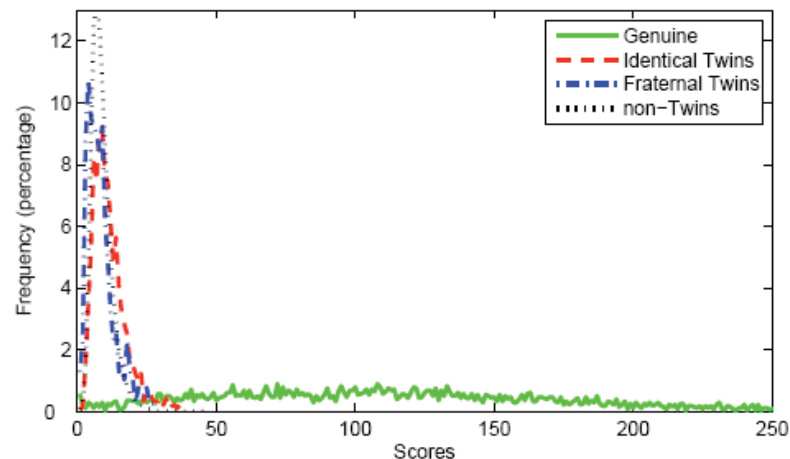


- Madrid Bomber case 22 minutiae identified
- 10 were matched by three FBI experts
- Generative Model
  - 12 of 19 minutiae used for specific nPRC: 1, 2, 3, 4, 7, 8, 9, 10, 11, 12, 17, and 18
  - specific nPRC
    - World population (6.8b) = 0.16
    - US population (330m) = 0.008



# Discriminative Models: Fingerprints

- Need a similarity measure for fingerprints
- AFIS Minutiae Matcher
  - Score distributions give two probabilities
  - Likelihood Ratio
- Error Rates



	EER	EER threshold
<b>Non-Twins</b>	3.33%	19
<b>Fraternal</b>	4.88%	23
<b>Identical</b>	5.09%	25

# Discriminative Model: QD

## Known

Nov. 10, 1999

From  
Jim Elder  
829 Loop Street, Apt. 300  
Allentown, New York 14707

To  
Dr. Bob Grant  
602 Queensberry Parkway  
Omar, West Virginia 25638

We were referred to you by Xena Cohen at the University Medical Center. This is regarding my friend, Kate Zack. It all started around six months ago while attending the "Rubeq" Jazz Concert. Organizing such an event is no picnic, and as President of the Alumni Association, a co-sponsor of the event, Kate was overworked. But she enjoyed her job, and did what was required of her with great zeal and enthusiasm.

However, the extra hours affected her health; halfway through the show she passed out. We rushed her to the hospital, and several questions, x-rays and blood tests later, were told it was just exhaustion.

Kates been in very bad health since. Could you kindly take a look at the results and give us yar opinion?

Thank You!

Jim

Letter shape

## Questioned

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Bigram shape

Word shape

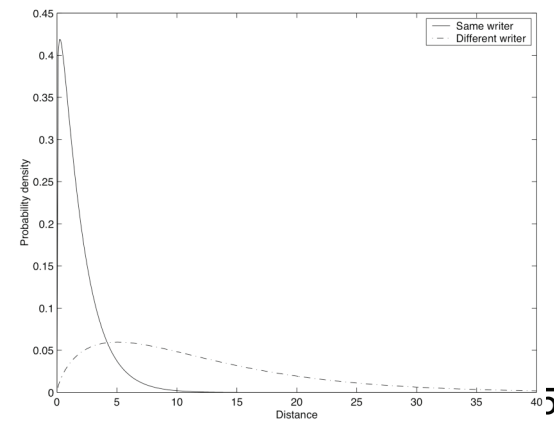
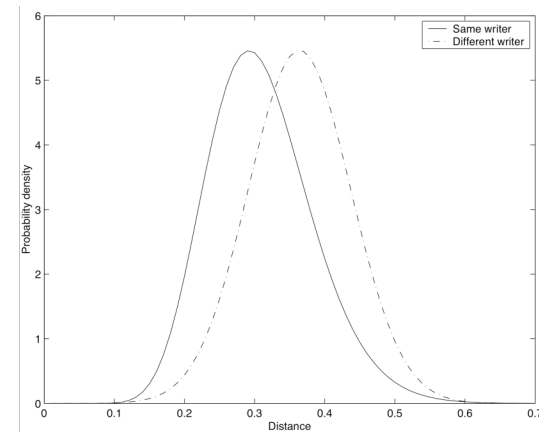
# Handwriting Features and Similarities



```
00000011011000000001100000011100
00000101000000110100001111000000
00001101000011110001010000000110
01100001100011000111000100000100
01000001000000000000000000000100
01100000000001000100000100011000
11000000000000000100101100011000
00000010000000001101000000000001
00000001111010000000001100000000
10100000000000110000001000100100
000000000000000000011000100000100
00000001000100000000000000000001
01110111111100010111001000000000
01010101000100010111001011110010
00000000110011100000000000000000
00000000000000000000000000000000
```

Likelihood Ratio  
obtained from  
distributions of  
similarities  
for same and different  
origination of evidence

## Distributions of Similarities



# Discriminative Model for Handwriting

However, the extra hours affected her health; halfway through the show she passed out. We rushed her to the hospital, and several questions, x-rays and blood tests later, we were told it was just exhaustion.

Kate has been in very bad health since. Could you kindly take a look at the results and give us your opinion?

Thank you!

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LLR Value for this pair is 41.52



1. Identified as same
2. Highly probable same
3. Probably same
4. Indicating same
5. No conclusion
6. Indicating different
7. Probably different
8. Highly probably different
9. Identified as different



# Human-Machine Interface: Dialog for character image comparison

Character ID: k

Character Type: Word Truthed

Questioned	Known	LLR Value
kindly in line 5	York in line 4	2.1425
kindly in line 5	Parkway in line 7	-0.2894
kindly in line 5	Zack in line 10	0.6211
take in line 5	York in line 4	-0.3098
take in line 5	Parkway in line 7	0.2085
take in line 5	Zack in line 10	0.9207
look in line 6	York in line 4	1.5929

Go Top

Page Up

Page Down

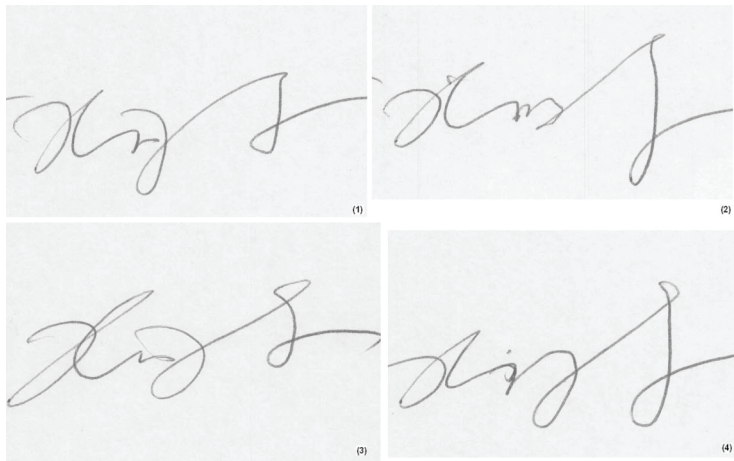
Go Bottom

OK

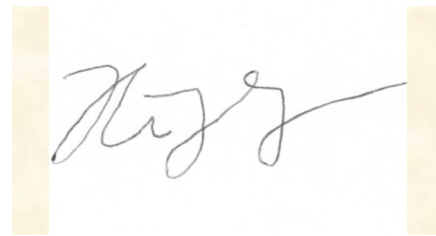
# Signatures: Bayesian Adaptation

Wide variability and small learning sets for case at hand

Known Signatures



Questioned Signature

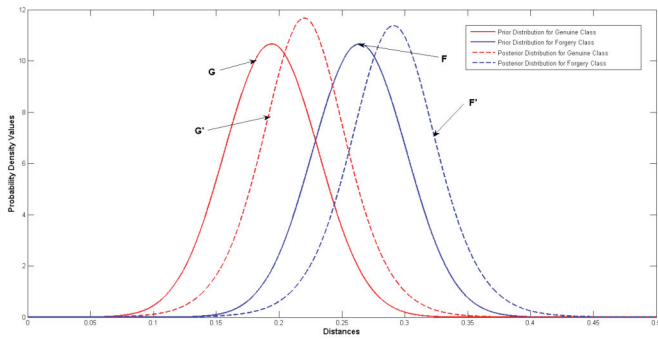


## Approach:

Learn hyper-parameters from large data set

Adapt parameters using Bayesian approach

# Bayesian Adaptation



	Error Rate
Only Prior	18%
Bayesian Adaptation	11.5% - 14.5%

	After Learning	After Adaptation
Parameter	$\theta_g \sim N(\mu_{g0}, \tau_{g0}^2)$ $\theta_f \sim N(\mu_{f0}, \tau_{f0}^2)$	$P(\theta_g   Y_g) \propto N(\theta_g   \mu_{g0}, \tau_{g0}^2) \times N(Y_g   \theta_g, \sigma_g^2) = N(\mu_g, \tau_g^2)$ $P(\theta_f   Y_f) \propto N(\theta_f   \mu_{f0}, \tau_{f0}^2) \times N(Y_f   \theta_f, \sigma_f^2) = N(\mu_f, \tau_f^2)$
Distance	$P(d_g   G) = \int_{-\infty}^{\infty} P(d_g   \theta_g) \times P(\theta_g   Y_g) d\theta_g = \frac{1}{\sqrt{2\pi(\sigma_g^2 + \tau_{g0}^2)}} e^{-\frac{(d_g - \mu_{g0})^2}{2(\sigma_g^2 + \tau_{g0}^2)}}$ $P(d_f   F) = \int_{-\infty}^{\infty} P(d_f   \theta_f) \times P(\theta_f   Y_f) d\theta_f = \frac{1}{\sqrt{2\pi(\sigma_f^2 + \tau_{f0}^2)}} e^{-\frac{(d_f - \mu_{f0})^2}{2(\sigma_f^2 + \tau_{f0}^2)}}$	$p(t/G) = \int_{-\infty}^{\infty} p(t   \theta_g) \times p(\theta_g   Y_g) d\theta_g = \frac{1}{\sqrt{2\pi(\sigma_g^2 + \tau_g^2)}} e^{-\frac{(t - \mu_g)^2}{2(\sigma_g^2 + \tau_g^2)}}$ $p(t/F) = \int_{-\infty}^{\infty} p(t   \theta_f) \times p(\theta_f   Y_f) d\theta_f = \frac{1}{\sqrt{2\pi(\sigma_f^2 + \tau_f^2)}} e^{-\frac{(t - \mu_f)^2}{2(\sigma_f^2 + \tau_f^2)}}$

# Summary and Conclusion

- Uncertainty is easily expressed for DNA
  - Discrete counts
- For Impression Evidence it is much harder
  - Continuous features/tolerances
- New Models proposed (being validated)
  - Generative
    - PRC
      - Fingerprints, Handwriting
  - Discriminative (similarity automatically computed)
    - Likelihoods/ Bayesian scores
      - Fingerprints, Handwriting