# Discussion of Three Papers on Treatment of Missing Data 

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## Introduction

- I enjoyed reading the three papers and listening to the presentations of them.
- First two papers (Fetter; Piela and Laaksonen): regression-based methods for imputing continuous and/or categorical missing data
- Third paper (Greene, Smith, Levenson, Hiser, and Mah): raking-based methods for handling missing data when the variables are categorical and form a contingency table with several dimensions and many cells
- I will discuss the first two papers first and discuss the third paper afterwards.


## Explicit models vs. implicit models

- Fetter's models:
- MCMI procedure based on explicit model
- RER procedure has both explicit (regression) and implicit (empirical residual) components
- Piela \& Laaksonen's models:
- CART procedures based on implicit models
- Implicit models often have a nonparametric flavor; attempt to be more robust
- Schenker and Taylor (1996) studied "partially parametric" techniques
- Results from Schenker and Taylor (1996, Table 4) on estimating the distribution function at the median, when the regression model underlying the multiple-imputation method is misspecified regarding the transformation of the outcome variable:

|  | Imputation Method |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  | Fully <br> Parametric | Predictive <br> Mean <br> Matching | Local <br> Residual <br> Draw | No <br> Missing <br> Data |
| MSE | 2.37 | 1.43 | 1.31 | 1.00 |
| Coverage of <br> Nominal <br> $95 \%$ Interval | 86.6 | 93.2 | 94.1 | 94.9 |

## Multiple imputation

- $M$ independent draws from

$$
p\left(Y_{m i s} \mid Y_{o b s}\right)=\int p\left(Y_{m i s} \mid Y_{o b s}, \boldsymbol{\theta}\right) p\left(\boldsymbol{\theta} \mid Y_{o b s}\right) d \boldsymbol{\theta}
$$

- For many models, can use two-step procedure to produce each draw of $Y_{m i s}$ :

1. Draw a value $\theta^{*}$ from $p\left(\theta \mid Y_{o b s}\right)$
2. Draw a value $Y_{\text {mis }}^{*}$ from $p\left(Y_{\text {mis }} \mid Y_{o b s}, \theta^{*}\right)$

- Can follow two-step paradigm for partially-parametric and/or nonparametric models
- e.g., for RER, for each of the $M$ sets of imputations, draw regression parameters from approximate posterior distribution prior to calculating predicted values and residuals (see Schenker and Taylor 1996)
- e.g., for each of the $M$ imputations of $Y_{m i s}$, run CART on a bootstrap sample to determine the tree


## Additional comments on Fetter

- Designed missing data to reduce respondent burden is an attractive idea
- Reminiscent of one-sixth sampling for census "long form"
- Consider one multivariate procedure for all of the logistic regressions?
- e.g., sequential regression imputation (Raghunathan et al. 2001)
- Might help to preserve relationships among the variables
- Don't forget to reflect uncertainty in estimating logistic regression parameters
- Unclear of the need to set some zero values to "missing" before running MCMI
- Could cause bias due to nonignorable missingness?
- Reason for lower precision of MCMI relative to RER?
- Seems preferable to condition on zero values
- Drawing from "local" empirical residuals rather than "global" empirical residuals might improve robustness to model misspecification (see Schenker and Taylor 1996)


## Additional comments on Piela and Laaksonen

- Potential for achieving robust imputations
- Can the method be used when there are missing values in the covariates?
- Difficult to judge performance based on one data set. Could just be "unlucky".
- Useful to examine performance under repeated sampling
- Useful to consider properties of inferences (multiple imputation?)
- Is it possible to build an assumption of nonignorable missing data into CART-based imputation?
- Problems with mode or mean imputation
- Distorts distribution of variables
- Biases when estimator is nonlinear in data
- Choosing the number of explanatory variables and the number of terminal nodes
- Bias/variance trade-off
- Analogous to choosing the number of donor cells in a hot-deck scheme
- Schenker and Taylor (1996) used an adaptive method for choosing the number of prospective donors for each missing value


## Comments on Greene et al.

- Greene et al. method has desirable properties relative to "national estimates method"
- All marginals are preserved
- Independent of ordering of variables
- Might be interesting to compare Greene et al. method with the "national estimates" method with respect to models underlying:
- contingency table
- missing-data mechanism
- Consider prior distributions to handle sparse data? - Rubin and Schenker (1987) and Clogg et al. (1991) discussed simple Bayesian methods for logistic regression
- Raking generally is useful when the marginal distributions for a table are known but the distributions inside the table are not known. In the application to fire data:
- How precisely are the marginals known?
- Could other methods for handling missing data in contingency tables be useful?
- Consider Table 1 of Greene et al. (this is Table 1 of the draft that was sent to me)

|  | Female | Male | Unknown | Total |
| :--- | ---: | ---: | ---: | ---: |
| Old | 65 | 30 | 5 | 100 |
| Young | 25 | 50 | 25 | 100 |
| Unknown | 10 | 2000 | 70 | 2080 |
|  | 100 | 2080 | 100 | 2280 |

- Marginal distribution of age not known very precisely, since 2080 values of age are missing
- Is it reasonable to distribute the $\mathbf{2 0 8 0}$ missing values on age 50/50 into young and old, and then treat the resulting marginals as the known "population" values for raking, as is done in Greene et al.?
- Note that 2000 of the missing values on age are for males
- Results of a few iterations of Greene et al. procedure:

|  | Female | Male | Total "Population" |  |
| :--- | ---: | ---: | ---: | ---: |
| Old | 84.3 | 1055.8 | 1140.1 | 1140.0 |
| Young | 20.6 | 1119.3 | 1139.9 | 1140.0 |
| Total | 104.9 | 2175.1 | 2280.0 | 2280.0 |
| "Population" | 104.6 | 2175.4 | 2280.0 |  |

- "Population" marginals preserved
- Odds ratio from original table preserved
- Distributions of age by gender from original table not preserved
- Some young females from original table "removed"; i.e., cell count for young females smaller than that in original table
- Results of a few iterations of EM algorithm (done by hand, with three significant digits of precision) for maximum likelihood under a saturated multinomial model, assuming ignorable missing data (see Little and Rubin 1987, Section 9.3):

|  | Female | Male | Total |
| :--- | ---: | ---: | ---: |
| Old | 74.9 | 798 | 873 |
| Young | 29.3 | 1378 | 1407 |
| Total | 104 | 2176 | 2280 |

- Gender marginals close to those for raking, but age marginals much different
- Odds ratio from original table nearly preserved
- Distributions of age by gender from original table nearly preserved
- Cell counts all greater than those in original table


## References

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