



# **AHRQ Present on Admission (POA) – Technical Overview**

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*2:00 to 3:30 pm ET*

*Toll Free: 1-877-939-8827; Passcode: AHRQ POA*



# AHRQ QI 2010 webinars to date

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## ■ January 12 and 14

- AHRQ QIs, Version 4.1 – Overview

## ■ January 25 and 27

- AHRQ QIs, Version 4.1 – Additional Detail

## ■ May 12

- AHRQ QIs use of Present on Admission – User Overview

## ■ May 14

- AHRQ QIs use of Present on Admission – Technical Overview



# Agenda

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- **POA Overview** (5 minutes)
  - Approach
- **POA Model Steps** (25 minutes)
  - Statistical Notation
  - Goal
  - Assumptions
  - Bayesian Approach
  - Data Imputation
  - Markov chain Monte Carlo (MCMC) Analysis
- **Software Tool** (5 minutes)
- **Example** (5 minutes)
- **Discussion** (30-45 minutes)



# POA Overview: Approach

- Two sets of algorithms needed to incorporate POA information
  - 1. Develop response variables and comorbidity factor covariates in the **presence** of POA data
    - Less measurement error thereby more accurate and based on fewer assumptions
  - 2. Develop response variables and comorbidity factor covariates in the **absence** of POA data
    - Use observed POA data to estimate probability of POA for response and comorbidity factors for patients that do not have POA data
    - Provide hospital with risk-adjusted rate that would be “most likely” had they collected POA data
- Observed and estimated data are used to develop the final AHRQ QI models



# POA Model Steps: Statistical Notation

- $Y_{ij}$  = PSI Indicator for the  $j^{\text{th}}$  patient in the  $i^{\text{th}}$  hospital
  - $Y_{ij}=1$  if the patient experiences the adverse health effect, 0 otherwise
- $P_{ij}$  = Indicator of whether the adverse health effect (represented by  $Y_{ij}$ ) is present on admission - determined from the POA data.
  - Note that  $P_{ij}$  will equal 0, by definition, if  $Y_{ij} = 0$ , but that  $P_{ij}$  could equal either 0 or 1 when  $Y_{ij} = 1$ .  $P_{ij}$  is not observed on everyone.
- $Z_{ij}$  = Vector of explanatory variables associated with the  $j^{\text{th}}$  patient in the  $i^{\text{th}}$  hospital, based on administrative records with no POA data.
  - $Z_{ij}$  is observed for everyone.
- $X_{ij}$  = Vector of improved explanatory variables associated with the  $j^{\text{th}}$  patient in the  $i^{\text{th}}$  hospital, based on administrative records with POA data.
  - $X_{ij}$  is not observed on everyone.



# POA Model Steps: Goal

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- Our goal is to predict:

$$\Pi_{ij} = \Pr(Y_{ij} = 1 | P_{ij} = 0, X_{ij})$$



# POA Model Steps: Assumptions

- Assume:  $Logit(\pi_{ij}) = X_{ij}\beta_Y + \delta_{Y,i}$
- Subcomponent of the model is prediction of :  
$$r_{ij} = \Pr[P_{ij} = 1 | X_{ij}]$$
  - Assume:  $Logit(r_{ij}) = X_{ij}\beta_P + \delta_{P,i}$



# POA Model Steps: Assumptions (cont.)

- Account for the anticipated within-hospital correlation among  $Y_{ij}$  responses, using a Generalized Estimating Equations (GEE) Approach
  - A random effects approach was considered, but was discarded because multiple observed hospitals with no cases were compromising the random effect estimates



# Likelihood Equations

- If POA data are available (and hence  $x_{ij}$  and  $P_{ij}$  are observed), we maximize the following likelihood, where  $r_{ij}$  is the probability that  $P=1$ , given the observable characteristics of  $X$ .

$$L_{ij} = \left( \pi_{ij}^{1-P_{ij}} \right)^{Y_{ij}} \left( 1 - \pi_{ij}^{1-P_{ij}} \right)^{1-Y_{ij}} r_{ij}^{P_{ij}} (1 - r_{ij})^{1-P_{ij}} [X_{ij}, Z_{ij}] \quad (i, j) \in \Omega,$$

- When  $x_{ij}$  and/or  $P_{ij}$  is not observed, we need to integrate/sum over the missing data  $P$  and  $X$ . Information about both of these may be obtained in the variables  $Z$  that are generally observed.

$$L_{ij} = \int_{X_{ij}} \sum_{P_{ij}} \left( \pi_{ij}^{1-P_{ij}} \right)^{Y_{ij}} \left( 1 - \pi_{ij}^{1-P_{ij}} \right)^{1-Y_{ij}} r_{ij}^{P_{ij}} (1 - r_{ij})^{1-P_{ij}} g(X_{ij}, Z_{ij}) \quad (i, j) \notin \Omega,$$

# Bayesian Approach

- Because  $X_{ij}$  can be  $>100$ , the integral equation is unfeasible
- To avoid calculating the integral
  - Use the following approach:

$$[\theta | W] \propto [W | \theta][\theta]$$

- If direct calculation of the likelihood is unfeasible can use MCMC sampling

# Data Estimation

- Combined use of Bayesian approach and other sampling techniques is convenient for missing data
- If  $\{\theta^{(j)}, W'^{(j)}\}_{j=1, \dots, n}$  is a random sample from  $[\theta, W' | W] \propto [W, W', \theta]^\xi$  then  $\{\theta^{(j)}\}_{j=1, \dots, n}$  is a random sample from  $[\theta | W] \propto [W, \theta] = \int_{W'} [W, W', \theta]$
- Allows sampling of augmented posterior distribution  $[W, W', \theta]$  rather than integration over missing data



# Model Fitting Approach using MCMC Overview

- Multiple pre-processing steps prior to fitting
  - Ensures data are formatted and sorted as anticipated
  - Eliminates columns of Z (and X) that are linearly dependent with each other
  - Allows for multiple P variables (i.e.,  $P_1, P_2, P_3$ ) – where  $P = \text{Max}(P_k)$
  
- MCMC Approach
  1. Establish  $X|Z$  using a series of 2x2 tables, and Establish  $P|X$  using a logistic regression modeling approach
  2. Impute values of X where missing using  $X|Z$ , and impute values of P where missing using  $P|X$  – creating an MCMC simulated analysis dataset
  3. Establish  $Y|X, P=0$  by fitting the logistic regression model  $Y|X$  for the subset of the MCMC simulated analysis dataset in which  $P=0$ .
    - Repeat steps 2-3 many times until parameter estimates reach convergence
  
- Analysis module fits the models two ways – using a Naïve simple logistic regression modeling approach, and using a GEE approach that accounts for within-hospital correlation

# Model Fitting Approach using MCMC Overview (cont.)

- Begin with

$$[Y, P, X, Z, P', X' | X' | \beta_Y, \delta_Y, \beta_P, \delta_P, \beta_Z] = [X | X'] [P | P'] \times [Y, P', X' Z] \beta_Y, \delta_Y, \beta_P, \delta_P, \beta_Z$$

- P' and X' indicate the “true process, such that  $Y = Y'$  and  $Z = Z'$  always, while for P and X, we set

$$[X | X'] [P | P'] = \prod_{(i,j) \in \Omega} \delta(X_{ij} - X'_{ij}) \prod_{(i,j) \in \Omega} \delta(P_{ij} - P'_{ij})$$

# Model Fitting Approach using MCMC (cont.)

- For the process model:

$$\begin{aligned} [Y, P', X', Z | \beta_Y, \delta_Y, \beta_P, \delta_P, \beta_Z] &= \prod_{ij} [Y_{ij} | P'_{ij}, X'_{ij}, \beta_Y, \delta_Y, i] \\ &\times \prod_{ij} [P'_{ij} | X'_{ij}, \beta_P, \delta_P, i] \\ &\times \prod_{ij} [X'_{ij} | Z_{ij}, \beta_x, ij] \\ &\times [Z] \end{aligned}$$

# Model Fitting Approach using MCMC (cont.)

- with  $[Y_{ij} | P'_{ij}, \beta_Y, \delta_{Y,i}] = (\pi_{ij}^{1-P'_{ij}})^{Y_{ij}} (1 - \pi_{ij}^{1-P'_{ij}})^{1-Y_{ij}}$   
 $[P'_{ij} | X'_{ij}, \beta_P, \delta_{P,i}] = r_{ij}^{P'_{ij}} (1 - r_{ij})^{1-P'_{ij}}$   
 $[X'_{ij} | Z'_{ij}, \beta_X, \delta_{X,ij}] = s_{ij}^{Z'_{ij}} (1 - s_{ij})^{1-Z'_{ij}}$
- Where  $\pi_{ij}$  and  $r_{ij}$  and  $\text{Logit}(s_{ij}) = \beta_{X,ij0} + Z_{ij} \beta_{X,ij1}$



# Model Fitting Approach using MCMC (cont.)

- Large number of parameters in the augmented likelihood and high percentage of missing P and X data, MCMC sampling may be unstable
  - Not representative of posterior parameter distribution
  - Need simplified model
    - Use logistic regression on subset of sample that have no missing data to consider them fixed during MCMC simulation
    - Gibbs (instead of Metropolis-Hasting)



# Model Fitting Approach using MCMC (cont.)

- Consider normal asymptotic expansion for fixed effects of logistic regression

$$\prod_{ij} (\pi_{ij}^{1-P'ij})(1 - \pi_{ij}^{1-P'ij})^{1-Yij} \approx N(\beta_Y, \delta_Y); (\hat{\beta}_Y, \hat{\delta}_Y), \hat{\Sigma})$$

- Run logistic regression on left hand side of equation above to create a set of parameters for normal function of right hand side of equation



# Model Fitting Approach using MCMC (cont.)

- To account for random hospital effects generalized estimated equations (GEE) theory is used to account for within-hospital correlation:

$$\prod_{ij} (\pi_{ij}^{1-P'ij})^{Y_{ij}} (1 - \pi_{ij}^{1-P'ij})^{1-Y_{ij}} \approx N(\beta_Y; \hat{\beta}_{GEE}, \hat{\Sigma}_{GEE})$$



# Model Fitting Approach using MCMC (cont.)

- In sum,
  - Use component-wise Metropolis-Hasting sampler, draw “true process” variables  $P'$  and  $X'$  according to augmented likelihood (use both data-model equations and process-model equations for estimation)
  - Use component-wise Gibbs sampler, draw fixed effect  $\beta_\gamma$  using a GEE normal approximation



# Model Fitting Approach using MCMC (cont.)

## ■ Linear Dependence

- Use singular value decomposition (SVD) to decompose the matrices:  $X^T X$  and  $Z^T Z$  using the kernel of matrix  $M = \text{kernel of } M^T M$ .

## ■ Separation

- MLE approach produces infinite estimates for certain fixed effects
- Use regularization term: ridge regression
- “Flat” normal prior distribution:

$$[\beta_Y] = N(\beta_Y; 0, I / \lambda)$$



# Model Fitting Approach using MCMC (cont.)

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- Estimate doesn't affect  $\beta_\gamma$  but stabilized the solution
- Improves instability due to residual collinearity in the data (i.e., not removed by SVD)

# Software Development

- Two Modules have been developed that implement the POA-Adjusted Quality Indicator Models
  - Analysis Module for fitting National data from the HCUP
    - Provides parameter estimates and associated standard errors from Naïve and GEE-based MCMC models:

$Y Z$	Similar to previously developed AHRQ Models
$P X$	Based on data where X is Observed
$Y X, P=0$	Based on data where X & P are Observed
$Y X, P=0$ (MCMC)	Based on Imputed data across entire dataset

- Prediction Module for applying Model Results to patient records from a select Hospital (or group of Hospitals)
  - Uses consistent MCMC approach to impute values of P and X (where missing) prior to applying parameter estimates – averaging the predicted values of Y over many simulations



# Software Development (cont.)

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- C++ program that implements MCMC simulations (patented by Battelle)
- Reads comma separated file containing the Y, P, X and Z data
- Eliminates zero and linearly dependent columns
- Performs GEE regression analyses on the distributions noted on last slide



# Software Development (cont.)

- Once coefficients fitted as appropriate performs standard and GEE analysis through MCMC with data estimation of the distribution  $[Y|P=0,X]$
- With more POA indicators a univariate value is calculated
- GEE regression (not MCMC simulation) “model standard errors” and “empirical standard errors” are calculated





# Software Development (cont.)

- After analysis, hospital predictions are calculated
- Software inputs: data filename; number of POA indicators; pathname of folder to store results; result filenames (standard regression analysis, GEE regression analysis, standard prediction results and GEE prediction results); subfolders to store various analytic files; analysis values, parameters and analytic steps; and, name of file to store log



# Software Development (cont.)

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- Prediction Module
  - The software tool can perform hospital aggregate predictions and individual predictions based on previous analyses

# Example

## ■ Postoperative Sepsis

tpps13/ qpps13 (P)	Discharges without POA Data	Discharges with POA Data		
	Missing	0	1	Total
0	549,614	248,629	0	798,243
1	8,208	2,312	1,436	11,956
Total	557,822	250,941	1,436	810,199
0	98.53%	98.51%	0.00%	98.51%
1	1.47%	0.92%	0.57%	1.49%
Total	100.00%	99.43%	0.57%	100.00%

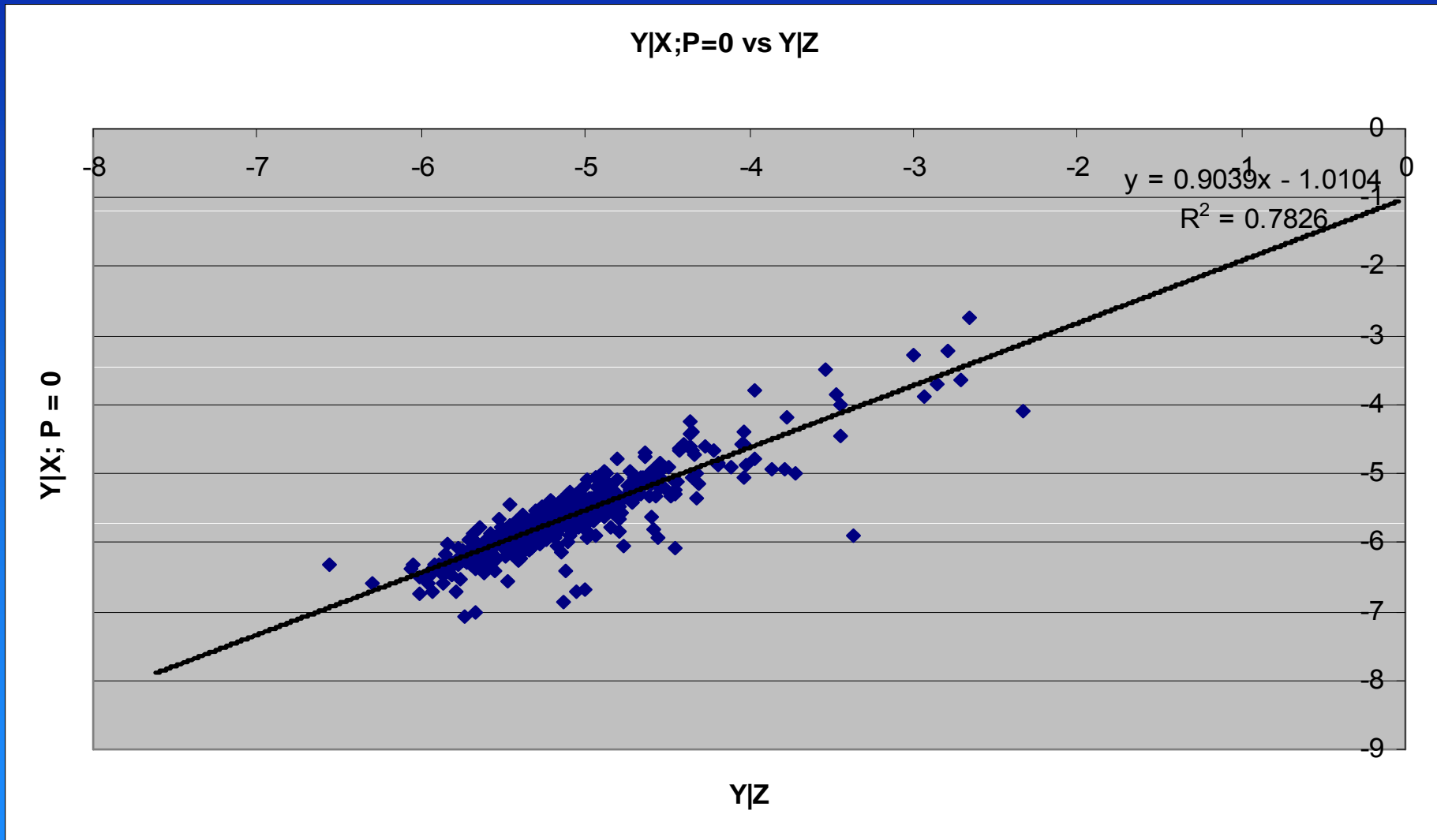
Table B2. Number and Percent of Discharges by Flag

Source: HCUP State Inpatient Databases (SID). Healthcare Cost and Utilization Project (HCUP). 2007. Agency for Healthcare Research and Quality, Rockville, MD. [www.hcup-us.ahrq.gov/sidoverview.jsp](http://www.hcup-us.ahrq.gov/sidoverview.jsp).

Note: tpps13 = inclusion in numerator; qpps13 = inclusion in denominator; (P) = cases flagged in outcome of interest excluded from population at risk because outcome is POA; 0 – does not meet inclusion; 1 = meets inclusion.

# Results: Postoperative Sepsis (current approach)

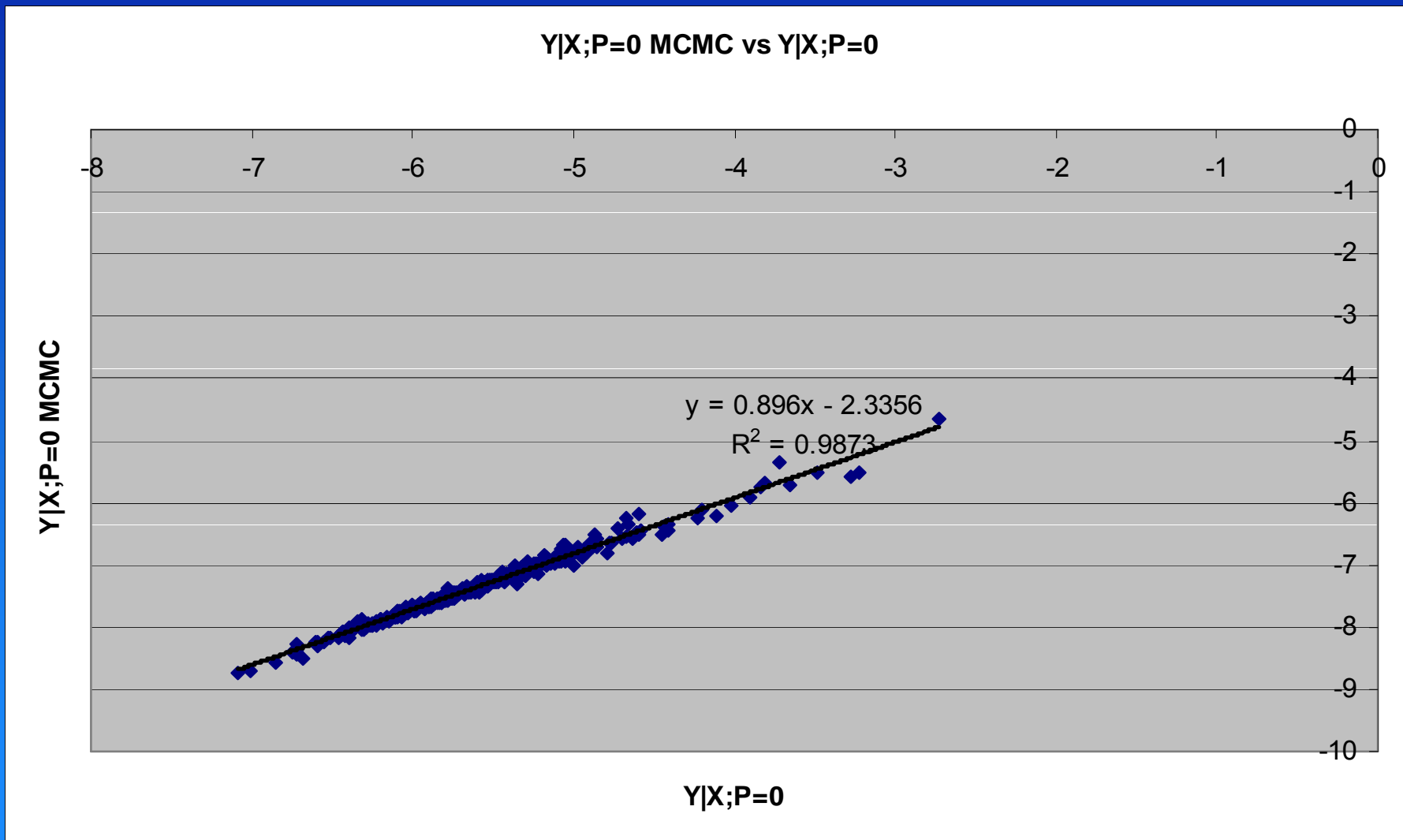
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Without POA

# Results: Postoperative Sepsis (Alternative approach)

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With POA



# Some Potential Next Steps

- Continue to refine the AHRQ QI numerator, denominator and risk factor definitions
  - Improve the sensitivity and specificity of the indicators
- Incorporate other tools to improve the coding of present on admission
  - Publicly available diagnostics on the accuracy of POA coding



# Discussion

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- For your consideration:
  - Did this webinar meet your needs?
    - Content? Scope?
  - How will the information presented be useful to you?
  - Is there anything we did not cover or didn't address in enough detail for you?
  
- Your questions:
  - Questions about what you heard today?
    - If we don't answer your question today, then we will post a response on the AHRQ QI website



# For more information...

## AHRQ QIs

- Web site: <http://qualityindicators.ahrq.gov/>
  - AHRQ QI documentation and software are available at the AHRQ QI web site
- Present on Admission White Paper:
  - <http://www.qualityindicators.ahrq.gov/downloads/webinars/Using%20Present%20on%20Admission.pdf>
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