COMPARTMENTAL ANALYSIS OF DRUG DISTRIBUTION



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DRUG DISTRIBUTION

The post-absorptive transfer of drug from one location in the body to another.

- Compartmental Models

 (ordinary differential equations)
- **Distributed Models**(partial differential equations)

Pharmacokinetic Models Using Ordinary Differential Equations*

MODEL	NUMBER OF COMPARTMENTS	MATHEMATICAL CHARACTERISTICS
NONCOMPARTMENTAL	0	CURVE FITTING TO DATA
COMPARTMENTAL	1-3	MODEL PARAMETERS FIT TO DATA
"PHYSIOLOGICAL"	4 - 20	MODEL PARAMETERS FIXED A PRIORI

^{*} From Atkinson AJ Jr, et al. Trends Pharmacol Sci 1991;12:96-101.

Mathematical vs. Physical Models*

MATHEMATICAL MODEL:

Functions or differential equations are employed without regard to the physical characteristics of the system.

PHYSICAL MODEL:

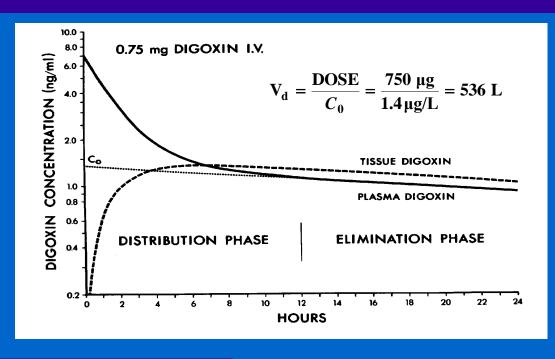
Implies certain mechanisms or entities that have physiological, biochemical or physical significance.

^{*} Berman M: The formulation and testing of models. Ann NY Acad Sci 1963;108:182-94

Goals of Drug Distribution Lecture

- Significance of Drug Distribution Volumes
- Physiological Basis of Multi-Compartment Pharmacokinetic Models
- Clinical Implications of Drug Distribution Kinetics

DIGOXIN DISTRIBUTION VOLUME



Body Fluid Spaces Catenary 3-Compartment Model Intravascular Space Intracellular Fluid Space capillaries cell membranes Elimination

Volume of Distribution and Physiological Fluid Spaces

Intravascular Space:

None

Extracellular Fluid Space:

Inulin

Proteins and other Macromolecules Neuromuscular Blocking Drugs (N⁺) Aminoglycoside Antibiotics (initially)

Volume of Distribution and Physiological Fluid Spaces

Total Body Water

Urea

Ethyl alcohol

Antipyrine (some protein binding)

Caffeine

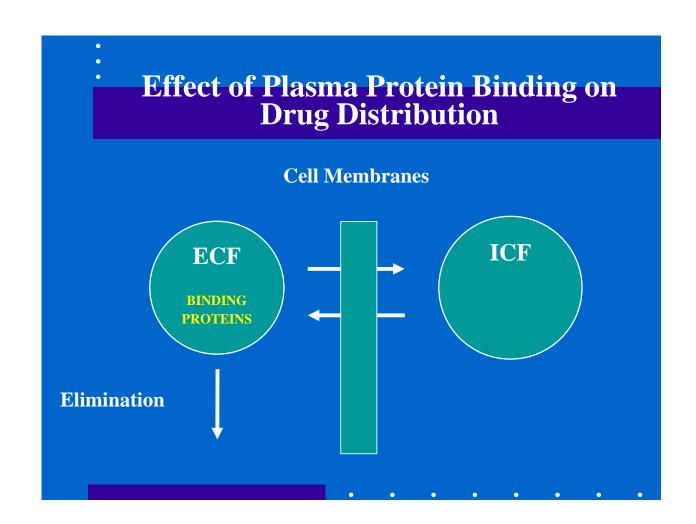
Factors Affecting Volume of Distribution Estimates

Binding to Plasma Proteins

Thyroxine Theophylline

Tissue Binding (partitioning)

Lipophilic Compounds Digoxin (Na⁺ - K⁺ ATPase)



Effect of Plasma Protein Binding on Apparent Volume of Distribution*

$$V_d = ECF + f_u(TBW - ECF)$$

 $\mathbf{f_u}$ is the "free fraction", the fraction of drug in plasma that is not bound to plasma proteins.

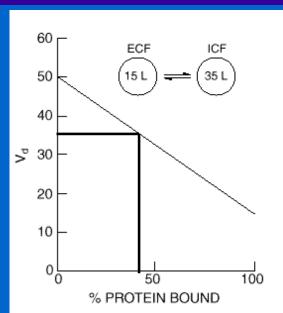
* Atkinson AJ Jr, et al. Trends Pharmacol Sci 1991;12:96-101.

Impact of Protein Binding on Thyroxine Distribution Volume* $f_{u} = 0.03\%$ $V_{d} = V_{ECF}$ $V_{d} = V_{ECF}$ * From Larsen PR, Atkinson AJ Jr, et al. J Clin Invest 1970;49:1266-79.

Impact of Protein Binding on Theophylline Distribution Volume*

$$f_u = 60\%$$

$$V_d = V_{ECF} + f_u V_{ICF}$$



* From Atkinson AJ Jr, et al. Trends Pharmacol Sci 1991;12:96-101.

Basis for Increased Theophylline Volume of Distribution in Pregnancy*

	f _U (%)	FLUID SPACE ESTIMATES (L)		TOTAL V _d (L)	
		ECF	TBW	EST.	MEAS.
PREGNANT					
24-26 WEEKS	88.9	13	34	32	30
36-38 WEEKS	87.0	21	40	38	37
POSTPARTUM					
6-8 WEEKS	77.4	12	33	28	28
>6 MONTHS	71.9	12	33	27	31

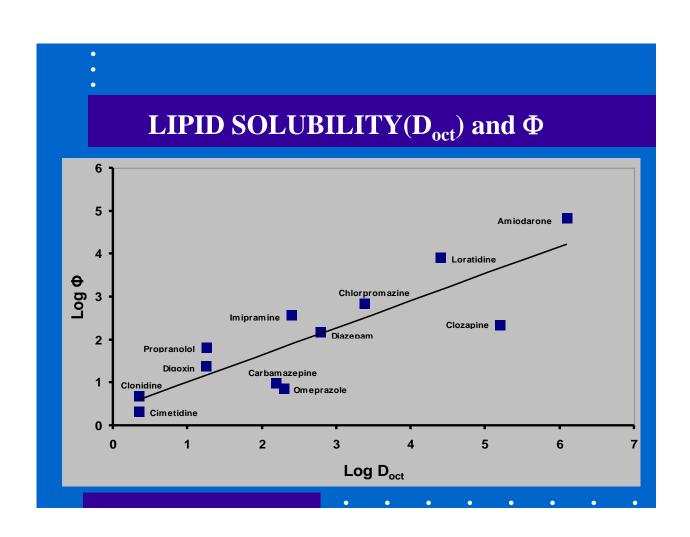
^{*} From Frederiksen MC, et al. Clin Pharmacol Ther 1986;40;321-8.

Effect of Plasma Protein and Tissue Binding on the Volume of Distribution of Most Drugs*

$$V_d = ECF + \Phi f_u (TBW - ECF)$$

 Φ is the ratio of tissue/plasma drug concentration.

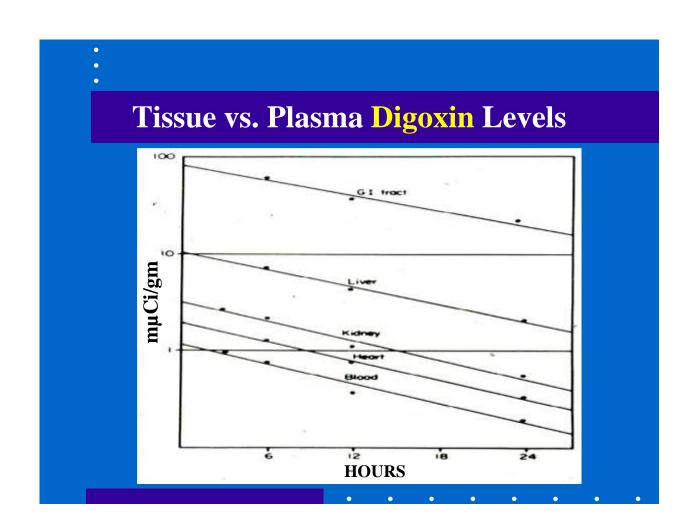
* Atkinson AJ Jr, et al. Trends Pharmacol Sci 1991;12:96-101.



Apparent Volume of Distribution for Digoxin

$$\begin{split} V_{d} &= ECF + \Phi f_{u} \big(TBW - ECF \big) \\ ECF &= 11.2 \text{ L}, \ TBW = 45.5 \text{ L}, \ f_{u} = 0.75 \text{ , } \Phi = 20.4 \\ V_{d} &= 11.2 + \big(20.4 \big) \big(0.75 \big) \big(34.3 \big) \text{ L} \\ V_{d} &= 536 \text{ L} \end{split}$$

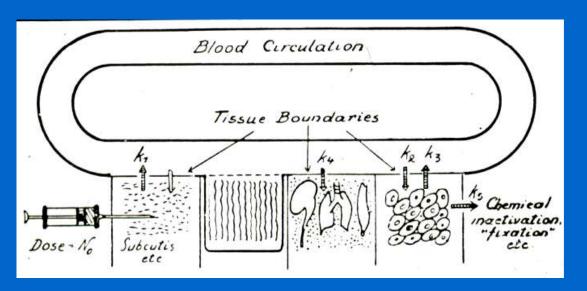
Φ includes binding to Na⁺-K⁺ATPase.



GOALS OF DRUG DISTRIBUTION LECTURE

- Significance of drug distribution volumes
- Physiologic basis of multi-compartment pharmacokinetic models
- Clinical implications of drug distribution kinetics

First Multicompartmental Analysis of Drug Distribution*

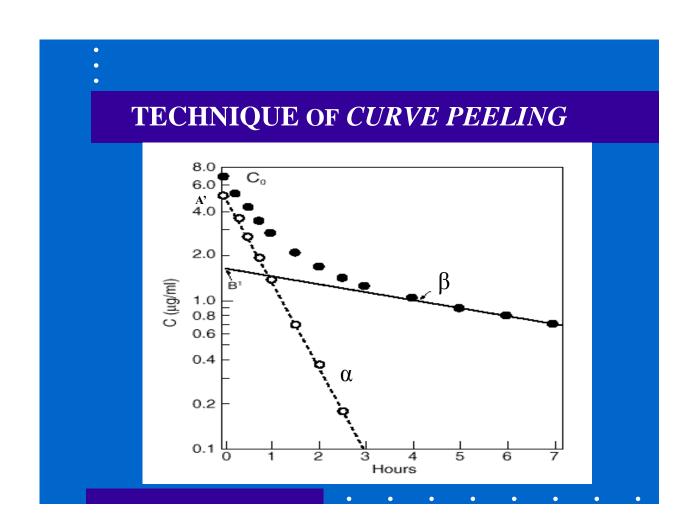


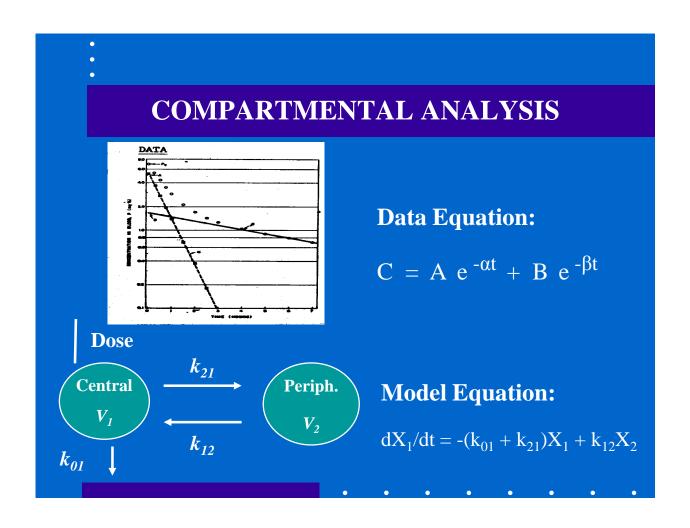
* From Teorell T. Arch Intern Pharmacodyn 1937;57:205-25.

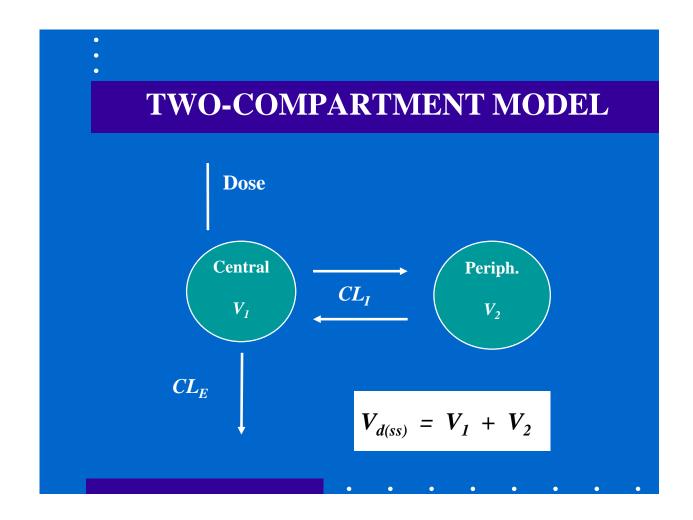
Analysis of Experimental Data

How many compartments?

Number of exponential phases in plasma level vs. time curve determines the number of compartments.



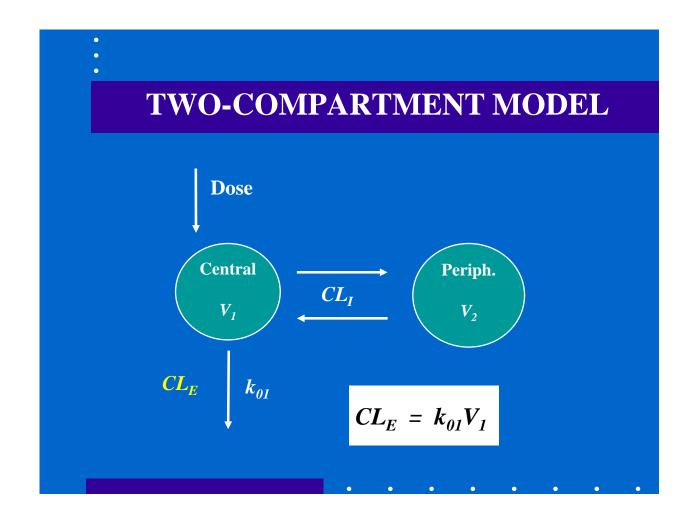




3 DISTRIBUTION VOLUMES

$$V_{d \text{ (extrap.)}} = \frac{DOSE/C_0}{V_{d \text{ (area)}}} = \frac{t_{1/2} \cdot CL_E}{0.693}$$

$$V_{d \text{ (ss)}} = V_1 + V_2 + \dots V_n$$



TWO-COMPARTMENT MODEL Dose k_{2l} V_l k_{12} CL_I CL_I

INTERCOMPARTMENTAL CLEARANCE*

Volume-Independent Parameter
Characterizing the Rate of Drug Transfer
Between Compartments of a Kinetic
Model

* From Saperstein et al. Am J Physiol 1955;181:330-6.

Is Central Compartment Intravascular Space?

- Usually not identified as such unless drug is given rapidly IV.
- NEED TO CONSIDER:
 - If distribution is limited to ECF, compare the central compartment volume with plasma volume.
 - If distribution volume exceeds ECF compare central compartment with blood volume.*

*(account for RBC/Plasma partition if [plasma] measured)

Analysis of Procainamide and NAPA Central Compartment Volumes*

DRUG	(L)			
	(L)		PREDICTED	OBSERVED
PA	6.7	1.52	5.6	5.5
NAPA	7.5	1.62	5.6	6.0

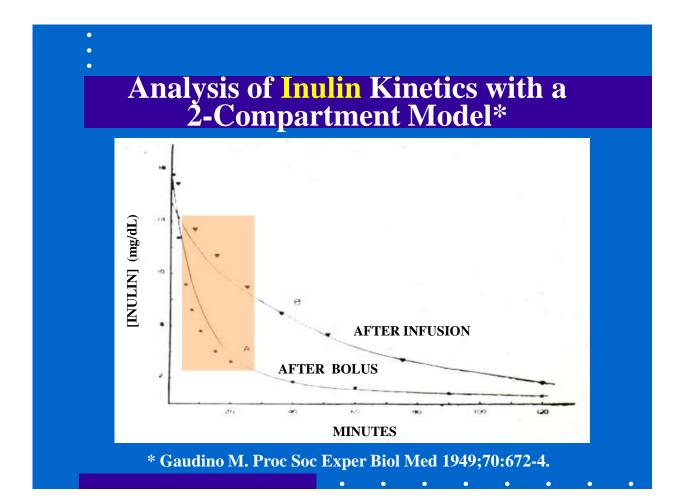
^{*} From Stec GP, Atkinson AJ Jr. J Pharmacokinet Biopharm 1981;9:167-80.

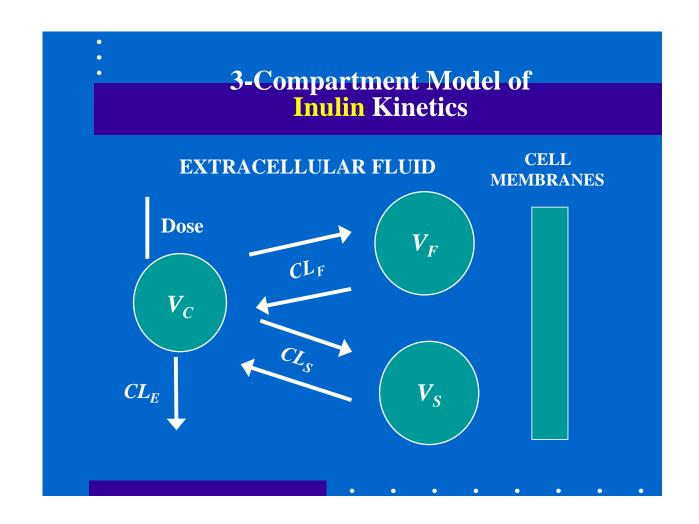
If Central Compartment Volume is Based on Plasma Concentration Measurements

$$\textbf{V}_{\text{\tiny C(corr.)}} = \textbf{V}_{\text{\tiny C(meas.)}} / \left[\left(\textbf{1-Hct} \right) + \textbf{Hct} \left(\textbf{RBC/P} \right) \right]$$

RBC/P = red cell/plasma partition ratio

Hct = hematocrit

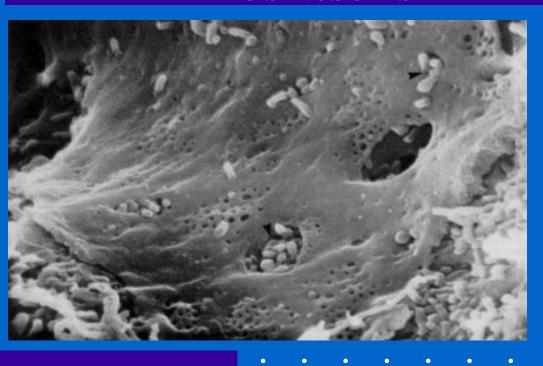




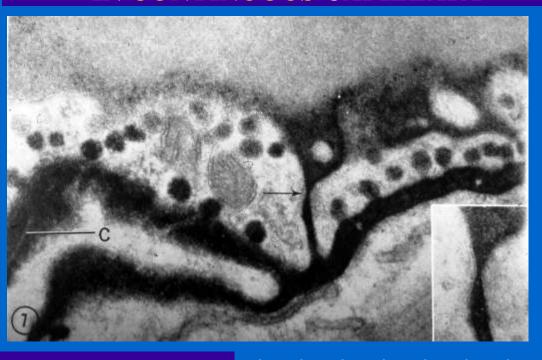
Basis for Kinetic Heterogeneity of Interstitial Fluid Space

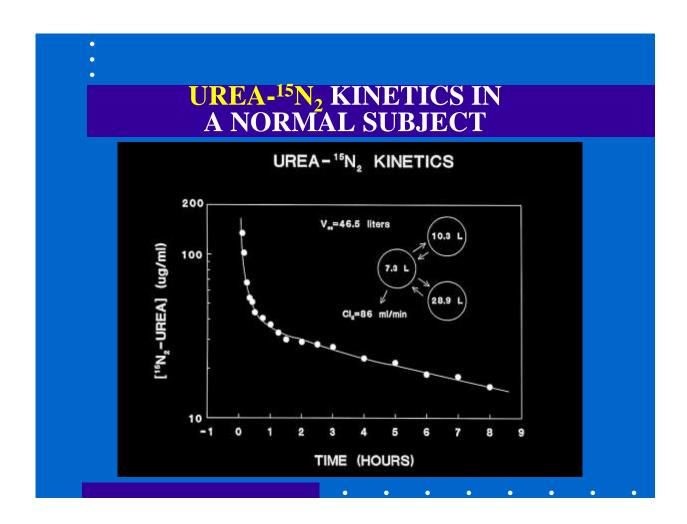
EFFECTIVE PORE SIZE	CAPILLARY STRUCTURE	PRIMARY LOCATION	
LARGE	FENESTRATED	SPLANCHNIC BED	
SMALL	CONTINUOUS	SOMATIC TISSUES	

ENDOTHELIAL FENESTRAE IN HEPATIC SINUSOIDS

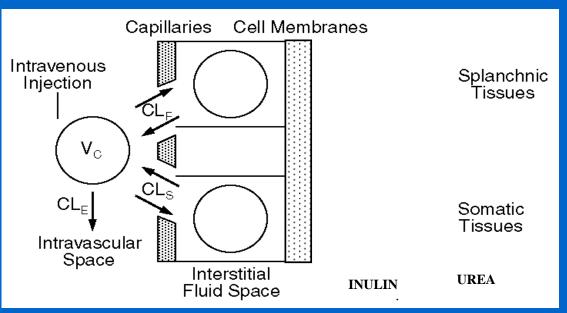


INTERENDOTHELIAL CELL JUNCTION IN CONTINUOUS CAPILLARY





Multicompartment Model of Inulin and Urea Kinetics*



* From Atkinson AJ Jr, et al. Trends Pharmacol Sci 1991;12:96-101.

ROLE OF TRANSCAPILLARY EXCHANGE

The central compartment for both urea and inulin is the intravascular space.

Therefore, transcapillary exchange is the ratelimiting step in the distribution of urea and inulin to the peripheral compartments of the mammillary 3-compartment model.

RENKIN EQUATION*

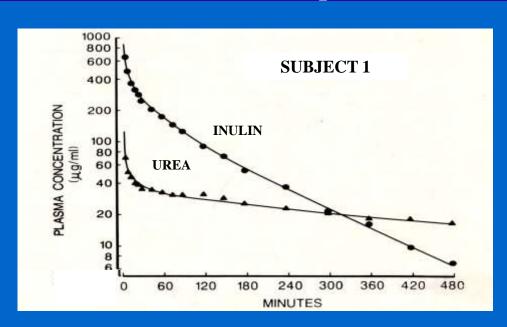
$$CI = Q(1-e^{-P/Q})$$

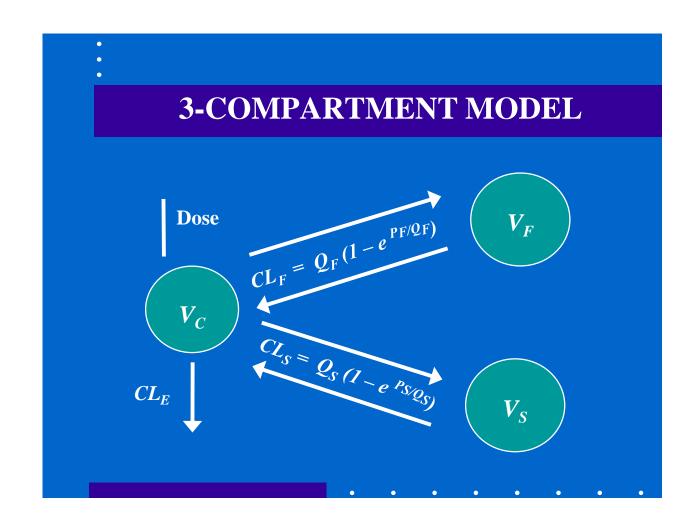
Q = capillary blood flow

P = capillary permeability coefficient-surface area product (sometimes denoted P•S).

* From Renkin EM. Am J Physiol 1953;183:125-36.

SIMULTANEOUS ANALYSIS OF INULIN AND UREA-15N₂ KINETICS





For Each Peripheral Compartment

3 UNKNOWNS:

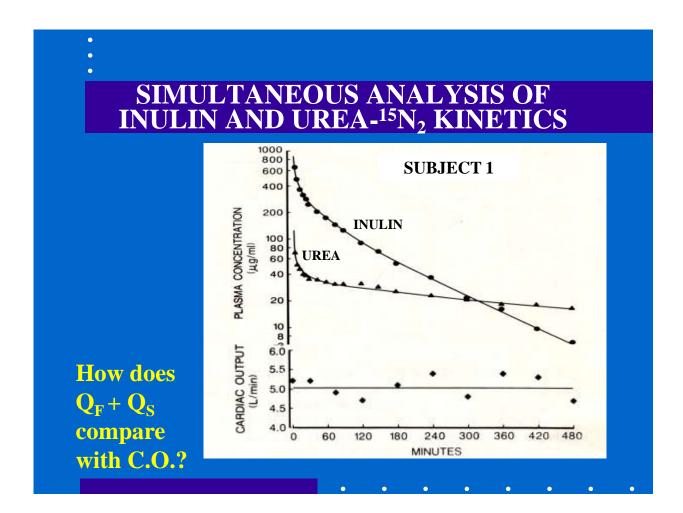
$$\mathbf{Q},\ \mathbf{P}_{\!\mathsf{U}},\ \mathbf{P}_{\!\mathsf{I}}$$

3 EQUATIONS:

$$\begin{aligned} & \mathbf{P_U} = \mathbf{Q} \; \mathbf{In} \big[\mathbf{Q} / \big(\mathbf{Q} - \mathbf{CI_U} \big) \big] \\ & \mathbf{P_I} = \mathbf{Q} \; \mathbf{In} \big[\mathbf{Q} / \big(\mathbf{Q} - \mathbf{CI_I} \big) \big] \\ & \mathbf{P_U} / \mathbf{P_I} = \; \mathbf{D_U} / \mathbf{D_I} \end{aligned}$$

U = urea; I = inulin

D = free water diffusion coefficient



CARDIAC OUTPUT AND COMPARTMENTAL BLOOD FLOWS*

	Q_{F}	Q _s	$Q_{F+}Q_{S}$	
	L/min	L/min	L/min	% CO
MEAN [†]	3.87	1.52	5.39	99

[†] MEAN OF 5 SUBJECTS

^{*} From Odeh YK, et al. Clin Pharmacol Ther 1993;53;419-25.

TRANSCAPILLARY EXCHANGE Mechanisms

TRANSFER OF SMALL MOLECULES (M.W. < 6,000 Da):

- Transfer proportional to D
 - Polar, uncharged (urea, inulin)
- Transfer rate < predicted from D
 - Highly charged (quaternary compounds)
 - Interact with pores (procainamide)
- Transfer rate > predicted from D
 - Lipid soluble compounds (anesthetic gases)
 - Facilitated diffusion (theophylline)

Urea and Theophylline Diffusion Coefficients*

	MOLECULAR WEIGHT	CORRECTED STOKES- EINSTEIN RADIUS	D _m @ 37° C
	(DALTONS)	(Å)	(x 10 ⁻⁵ cm ² /sec)
UREA	60	2.2	1.836
THEOPHYLLINE	180	3.4	1.098

^{*} From Belknap SM, et al. J Pharmacol Exp Ther 1987;243;963-9.

PRESUMED CARRIER-MEDIATED TRANSCAPILLARY EXCHANGE

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- Physiologic basis of multi-compartment pharmacokinetic models
- Clinical implications of drug distribution kinetics

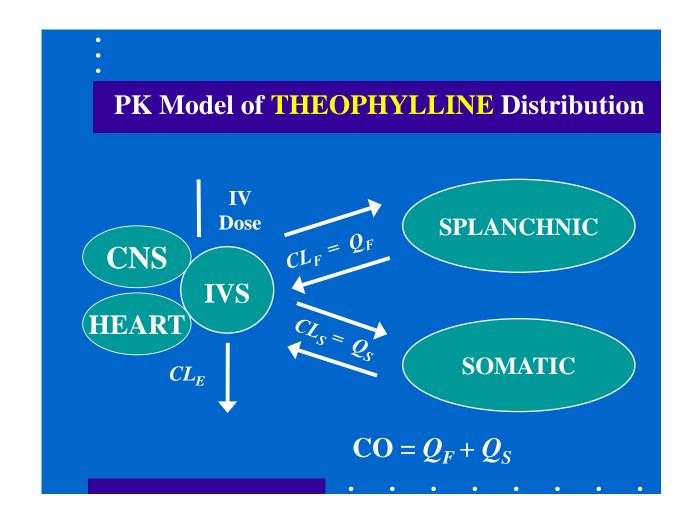
SIGNIFICANCE OF DRUG DISTRIBUTION RATE

1. Affects toxicity of IV injected drugs

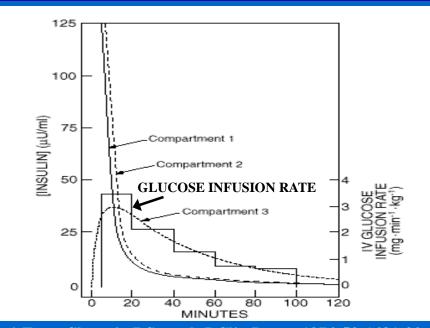
Theophylline, lidocaine

- 2. Delays onset of drug action Insulin, digoxin
- 3. Terminates action after IV bolus dose

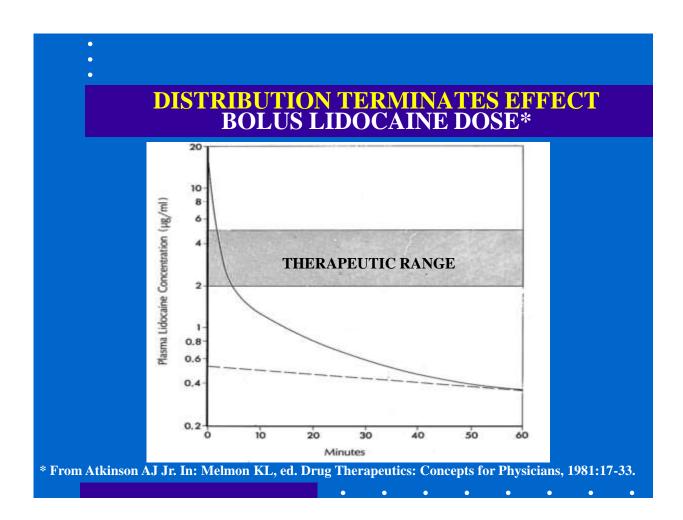
Thiopental, lidocaine



PK-PD Study of INSULIN Enhancement of Skeletal Muscle Glucose Uptake*

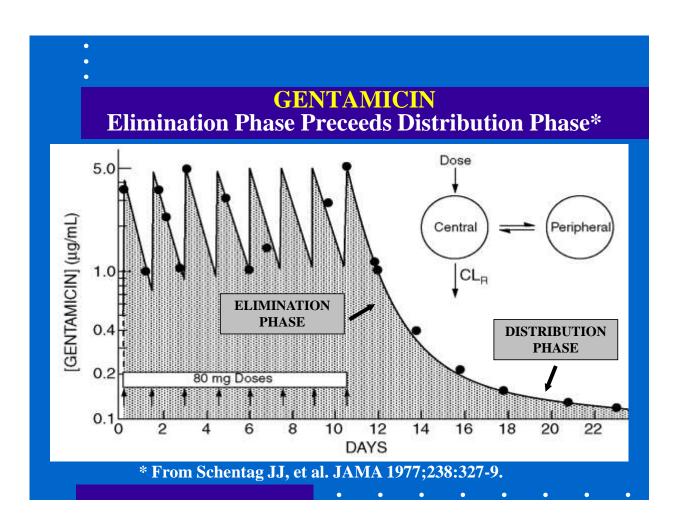


* From Sherwin RS, et al. J Clin Invest 1974;53:1481-92.



CONSEQUENCES OF VERY SLOW DRUG DISTRIBUTION

- "Flip-Flop" Kinetics
- Effective Half-Life
- Pseudo Dose Dependency

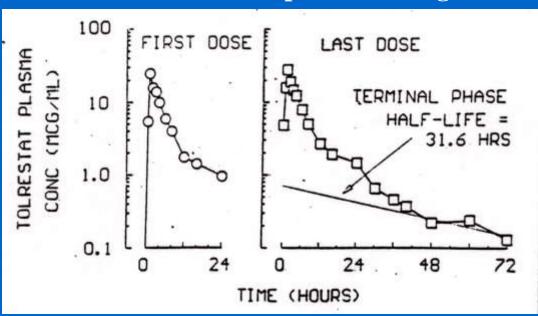


GENTAMICIN ELIMINATION Nephrotoxic vs. Non-Toxic Patient* NEPHROTOXIC NON-TOXIC NON-TOXIC Paris Section 1978;6:179-86.

CONSEQUENCES OF VERY SLOW DRUG DISTRIBUTION

- "Flip-Flop" Kinetics
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TOLRESTAT Cumulation with Repeated Dosing*



*From Boxenbaum H, Battle M: J Clin Pharmacol 1995;35:763-6.

CUMULATION FACTOR

$$CF = \frac{1}{\left(1 - e^{-k\tau}\right)}$$

TOLRESTAT CUMULATION

Predicted C.F. from $T_{1/2} = 31.6 \text{ hr}$: 4.32

Observed C.F.: 1.29

EFFECTIVE HALF- LIFE*

$$k_{eff} = \frac{1}{\tau} ln \left(\frac{CF_{obs}}{CF_{obs} - 1} \right)$$

$$t_{\frac{1/2\,\text{eff}}{}} = \frac{ln2}{k_{\frac{eff}{}}}$$

* From Boxenbaum H, Battle M. J Clin Pharmacol 1995;35:763-66.

EFFECTIVE HALF-LIFE OF TOLRESTAT*

Since $\tau = 12$ hr and Observed CF = 1.29:

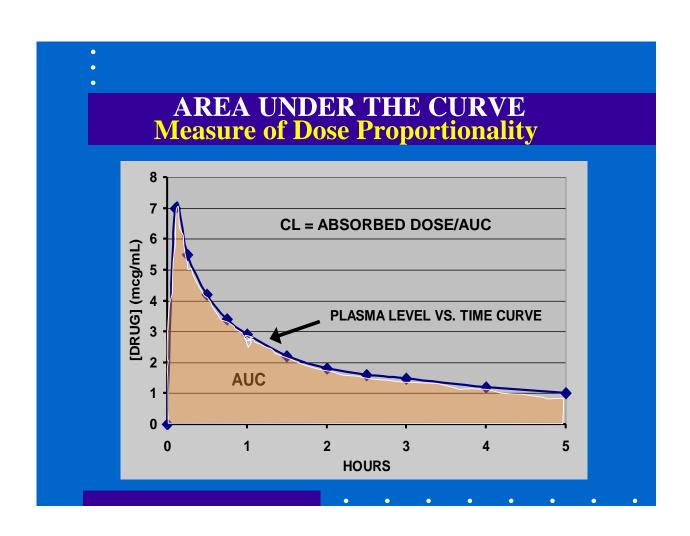
$$k_{eff} = \frac{1}{12} \ln \left(\frac{1.29}{1.29 - 1} \right) = 0.124 \text{ hr}^{-1}$$

$$t_{1/2eff} = \frac{\ln 2}{0.124} = 5.6 \text{ hr}$$

^{*} From Boxenbaum H, Battle M. J Clin Pharmacol 1995;35:763-66.

CONSEQUENCES OF VERY SLOW DRUG DISTRIBUTION

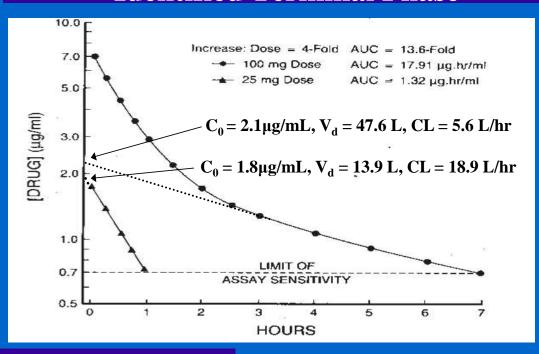
- "Flip-Flop" Kinetics
- Effective Half-Life
- Pseudo Dose Dependency



HYPOTHETICAL Phase I Trial Results

	DOSE 1	DOSE 2	INCREASE
DOSE (mg)	25	100	4 x ↑
AUC (μg-hr/mL)	1.32	17.91	13.6 x ↑

Dependency of PK Estimates on Identified Terminal Phase



DISTRIBUTION VOLUME Representative Macromolecules

MACROMOLECULE	MW (kDa)	V ₁ (mL/kg)	V _{d(ss)} (mL/kg)
INULIN	5.2	55	164
FACTOR IX (FIX)	57	136	271
INTERLEUKIN-2 (IL-2)	15.5	60	112
INTERLEUKIN-12 (IL-12)	53	52	59
GRANULOCYTE COLONY STIMULATING FACTOR (G-CSF)	20	44	60
RECOMBINANT TISSUE PLASMINOGEN ACTIVATOR (RT-PA)	65	59	106

CLOTTING FACTOR PHARMACOKINETICS*

- "The V_{d(ss)}..... always exceeds the actual plasma volume, implying that no drug, not even large molecular complexes as F-VIII, is entirely confined to the plasma space."
- "A too short blood sampling protocol gives flawed results not only for terminal T1/2 but also for the model independent parameters."
- * Berntorp E, Björkman S. Haemophilia 2003;9:353-9.