#### COMPARTMENTAL ANALYSIS OF DRUG DISTRIBUTION



Juan J.L. Lertora, M.D., Ph.D.
Director

Director
Clinical Pharmacology Program
September 23, 2010

Office of Clinical Research Training and Medical Education National Institutes of Health Clinical Center

#### **DRUG DISTRIBUTION**

The post-absorptive transfer of drug from one location in the body to another.

- Compartmental Models
  (ordinary differential equations)
- Distributed Models
  (partial differential equations)

#### Pharmacokinetic Models Using Ordinary Differential Equations\*

MODEL	NUMBER OF COMPARTMENTS	MATHEMATICAL CHARACTERISTICS
NONCOMPARTMENTAL	0	CURVE FITTING TO DATA
COMPARTMENTAL	1-3	MODEL PARAMETERS FIT TO DATA
"PHYSIOLOGICAL"	4 - 20	MODEL PARAMETERS FIXED A PRIORI

\* From Atkinson AJ Jr, et al. Trends Pharmacol Sci 1991;12:96-101.

### Mathematical vs. Physical Models\*

Functions or differential equations are employed without regard to the physical characteristics of the system.

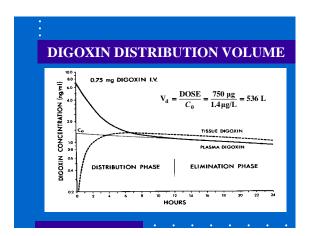
#### **PHYSICAL MODEL:**

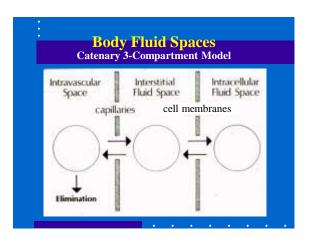
Implies certain mechanisms or entities that have physiological, biochemical or physical significance.

\* Berman M: The formulation and testing of models. Ann NY Acad Sci 1963;108:182-94

#### **Goals of Drug Distribution Lecture**

- Significance of Drug Distribution Volumes
- Physiological Basis of Multi-Compartment Pharmacokinetic Models
- Clinical Implications of Drug Distribution Kinetics





#### Volume of Distribution and Physiological Fluid Spaces

#### **Intravascular Space:**

None

#### **Extracellular Fluid Space:**

#### Inulin

Proteins and other Macromolecules Neuromuscular Blocking Drugs (N+) Aminoglycoside Antibiotics (initially)

#### Volume of Distribution and Physiological Fluid Spaces

#### **Total Body Water**

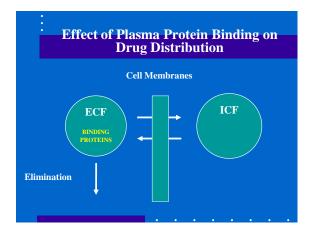
Urea

**Ethyl alcohol** 

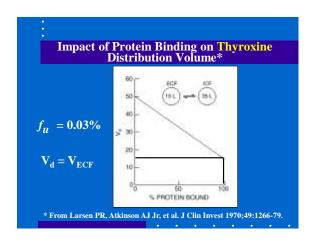
Antipyrine (some protein binding)

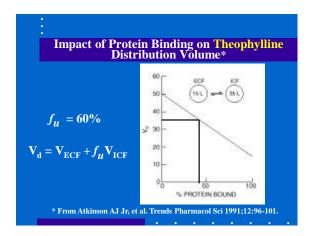
Caffeine

# Factors Affecting Volume of Distribution Estimates Binding to Plasma Proteins Thyroxine Theophylline Tissue Binding (partitioning) Lipophilic Compounds Digoxin (Na+ - K+ATPase)

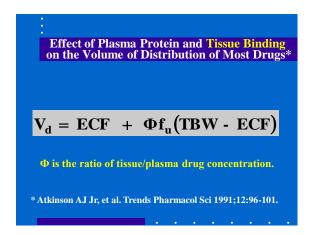


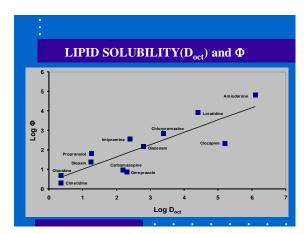
Effect of Pla	asma Protein Binding on Volume of Distribution*
$V_d = ECF$	+ f <sub>u</sub> (TBW - ECF)
f <sub>u</sub> is the "free fractio that is not bound to p	on", the fraction of drug in plasma plasma proteins.

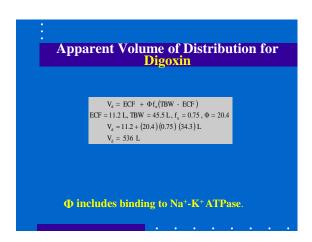


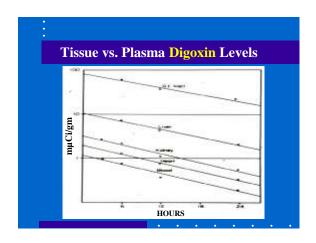


Basis f	or Inc f Disti	reased ibutio	Theop n in Pr	hyllin egnar	e icy*
	f <sub>U</sub> (%)	FLUID SPACE ESTIMATES (L)		TOTAL V <sub>d</sub> (L)	
		ECF	TBW	EST.	MEAS.
PREGNANT					
24-26 WEEKS	88.9	13	34	32	30
36-38 WEEKS	87.0	21	40	38	37
POSTPARTUM					
6-8 WEEKS	77.4	12	33	28	28
>6 MONTHS	71.9	12	33	27	31



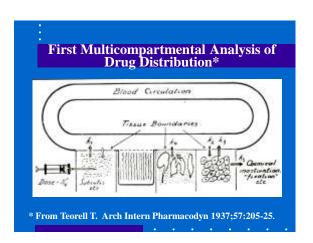




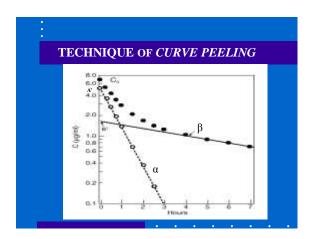


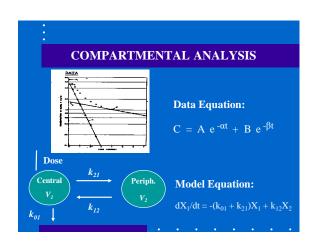
#### GOALS OF DRUG DISTRIBUTION LECTURE

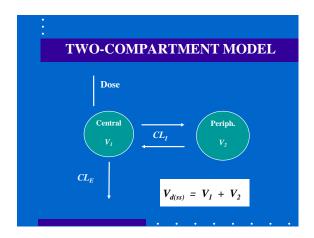
- Significance of drug distribution volumes
- Physiologic basis of multi-compartment pharmacokinetic models
- Clinical implications of drug distribution kinetics



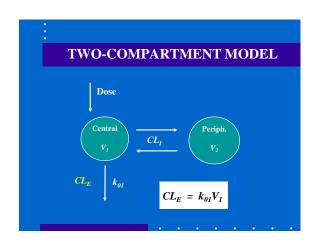
## Analysis of Experimental Data How many compartments? Number of exponential phases in plasma level vs. time curve determines the number of compartments.

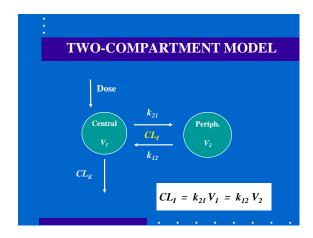






# 3 DISTRIBUTION VOLUMES $V_{d \text{ (extrap.)}} = \frac{DOSE}{C_0}$ $V_{d \text{ (area)}} = \frac{t_{1/2} \cdot CL}{0.693}$ $V_{d \text{ (ss)}} = V_1 + V_2 + \dots V_n$





#### INTERCOMPARTMENTAL CLEARANCE\*

Volume-Independent Parameter
Characterizing the Rate of Drug Transfer
Between Compartments of a Kinetic
Model

\* From Saperstein et al. Am J Physiol 1955;181:330-6.

#### Is Central Compartment Intravascular Space?

- Usually not identified as such unless drug is given rapidly IV.
- NEED TO CONSIDER:
  - If distribution is limited to ECF, compare the central compartment volume with plasma volume.
  - If distribution volume exceeds ECF compare central compartment with blood volume.\*

\*(account for RBC/Plasma partition if [plasma] measured)

#### Analysis of Procainamide and NAPA Central Compartment Volumes\*

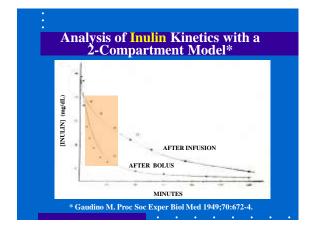
DRUG	V <sub>c</sub> (L)	RBC/P	INTRAVASCU (I PREDICTED	LAR SPACE L) OBSERVED
PA	6.7	1.52	5.6	5.5
NAPA	7.5	1.62	5.6	6.0

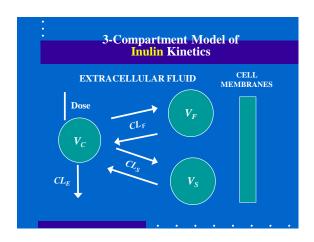
\* From Stee GP, Atkinson AJ Jr. J Pharmacokinet Biopharm 1981;9:167-80.

If Central Compartment Volume is Based on Plasma Concentration Measurements

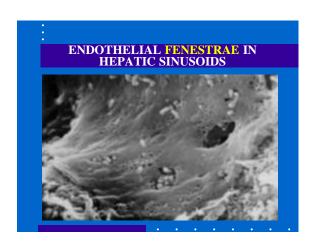
$$\textbf{V}_{\text{C(corr.)}} \ = \ \textbf{V}_{\text{C(meas.)}} \ / \left[ \left( 1 \! - \! \text{Hct} \right) + \ \text{Hct} \left( \text{RBC} \middle/ P \right) \right]$$

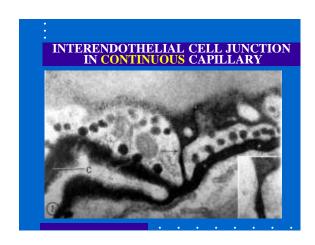
RBC/P = red cell/plasma partition ratio Hct = hematocrit

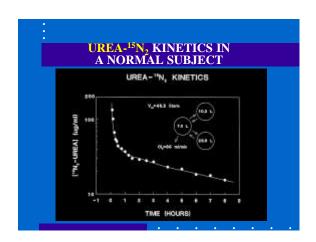


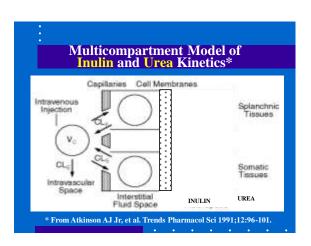


	netic Heteroge Fluid Spa	ice
		ı
EFFECTIVE PORE SIZE	CAPILLARY STRUCTURE	PRIMARY LOCATION
LARGE	FENESTRATED	SPLANCHNIC BEI
SMALL	CONTINUOUS	SOMATIC TISSUES









#### ROLE OF TRANSCAPILLARY EXCHANGE

The central compartment for both urea and inulin is the intravascular space.

Therefore, transcapillary exchange is the ratelimiting step in the distribution of urea and inulin to the peripheral compartments of the mammillary 3-compartment model.

#### **RENKIN EQUATION\***

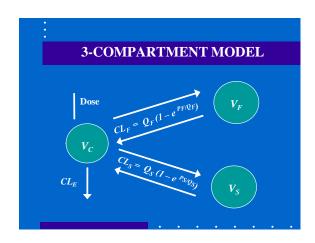
$$CI = Q(1-e^{-P/Q})$$

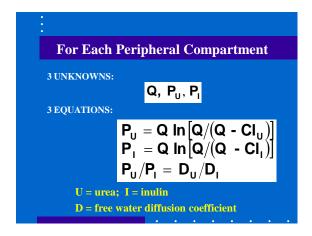
Q = capillary blood flow

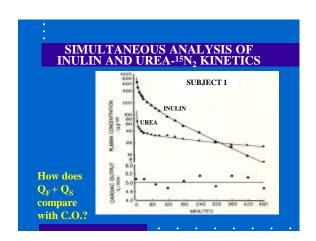
P = capillary permeability coefficient-surface area product (sometimes denoted P•S).

\* From Renkin EM. Am J Physiol 1953;183:125-36.

# SIMULTANEOUS ANALYSIS OF INULIN AND UREA-15N<sub>2</sub> KINETICS SUBJECT 1 SUBJECT 1 INULIN WEA SUBJECT 1 MENUTES







#### CARDIAC OUTPUT AND COMPARTMENTAL BLOOD FLOWS\*

	$Q_F$	Q <sub>s</sub>	Q <sub>F+</sub> Q <sub>S</sub>		
	L/min	L/min	L/min	% CO	
MEAN <sup>†</sup>	3.87	1.52	5.39	99	

- † MEAN OF 5 SUBJECTS
- \* From Odeh YK, et al. Clin Pharmacol Ther 1993;53;419-25.

#### TRANSCAPILLARY EXCHANGE Mechanisms

#### TRANSFER OF SMALL MOLECULES (M.W. < 6,000 Da):

- Transfer proportional to D
- Polar, uncharged (urea, inulin)
- Transfer rate < predicted from D
- Highly charged (quaternary compounds)
- Interact with pores (procainamide)
- $\bullet$  Transfer rate > predicted from D
- Lipid soluble compounds (anesthetic gases)
- Facilitated diffusion (theophylline)

#### Urea and Theophylline Diffusion Coefficients\*

	MOLECULAR WEIGHT	CORRECTED STOKES- EINSTEIN RADIUS	D <sub>m</sub> @ 37° C
	(DALTONS)	(Å)	(x 10 <sup>-5</sup> cm <sup>2</sup> /sec)
UREA	60	2.2	1.836
THEOPHYLLINE	180	3.4	1.098

\* From Belknap SM, et al. J Pharmacol Exp Ther 1987;243;963-9.

#### GOALS OF DRUG DISTRIBUTION LECTURE

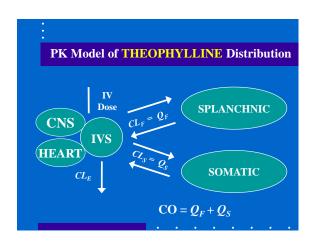
- Significance of drug distribution volumes
- Physiologic basis of multi-compartment pharmacokinetic models
- Clinical implications of drug distribution kinetics

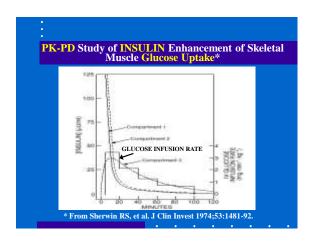
#### SIGNIFICANCE OF DRUG DISTRIBUTION RATE

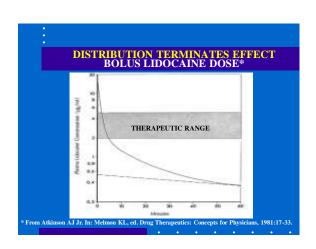
1. Affects toxicity of IV injected drugs

Theophylline, lidocaine

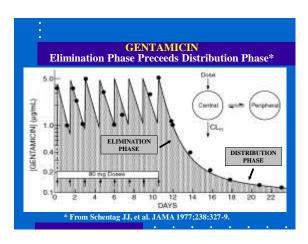
- 2. Delays onset of drug action Insulin, digoxin
- $\begin{tabular}{ll} {\bf 3.} & {\bf Terminates} & {\bf action} & {\bf after} & {\bf IV} & {\bf bolus} & {\bf dose} \\ \\ & {\bf Thiopental, lidocaine} & \\ \end{tabular}$

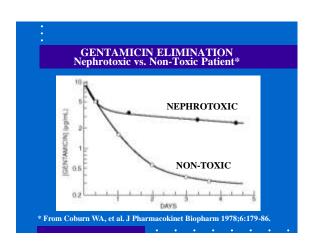




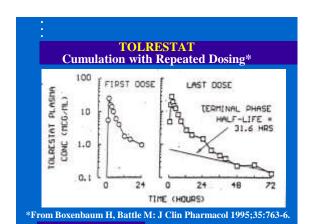


### 





### CONSEQUENCES OF VERY SLOW DRUG DISTRIBUTION • "Flip-Flop" Kinetics • Effective Half-Life



• Pseudo Dose Dependency

## CUMULATION FACTOR $CF = \frac{1}{\left(1 - e^{-k\tau}\right)}$

#### TOLRESTAT CUMULATION

Predicted C.F. from  $T_{1/2} = 31.6 \text{ hr}$ : 4.32

Observed C.F.: 1.29

#### **EFFECTIVE HALF-LIFE\***

$$k_{eff} = \frac{1}{\tau} ln \left( \frac{CF_{obs}}{CF_{obs} - 1} \right)$$

$$t_{1/2\text{eff}} = \frac{\ln 2}{k_{\text{eff}}}$$

\* From Boxenbaum H, Battle M. J Clin Pharmacol 1995;35:763-66.

#### **EFFECTIVE HALF-LIFE OF TOLRESTAT\***

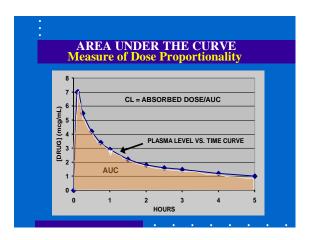
Since  $\tau = 12$  hr and Observed CF = 1.29:

$$k_{eff} = \frac{1}{12} \ln \left( \frac{1.29}{1.29 - 1} \right) = 0.124 \text{ hr}^{-1}$$

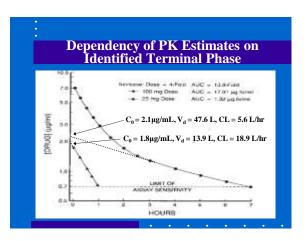
$$t_{1/2eff} = \frac{\ln 2}{0.124} = 5.6 \text{ hr}$$

\* From Boxenbaum H, Battle M. J Clin Pharmacol 1995;35:763-66.

### 



		HYPOT Phase I T	HETICAI Trial Resul	lts	
		DOSE 1	DOSE 2	INCREASE	
	DOSE (mg)	25	100	4 x ↑	
(µ	AUC ig-hr/mL)	1.32	17.91	13.6 x ↑	



: DISTRIBUTION VOLUME Representative Macromolecules					
MACROMOLECULE	MW (kDa)	V <sub>1</sub> (mL/kg)	V <sub>d(ss)</sub> (mL/kg)		
INULIN	5.2	55	164		
FACTOR IX (FIX)	57	136	271		
INTERLEUKIN-2 (IL-2)	15.5	60	112		
INTERLEUKIN-12 (IL-12)	53	52	59		
GRANULOCYTE COLONY STIMULATING FACTOR (G-CSF)	20	44	60		
RECOMBINANT TISSUE PLASMINOGEN ACTIVATOR (RT-PA)	65	59	106		

#### CLOTTING FACTOR PHARMACOKINETICS\*

- "The V<sub>d(ss)</sub>..... always exceeds the actual plasma volume, implying that no drug, not even large molecular complexes as F-VIII, is entirely confined to the plasma space."
- "A too short blood sampling protocol gives flawed results not only for terminal T1/2 but also for the model independent parameters."
- \* Berntorp E, Björkman S. Haemophilia 2003;9:353-9.